Sponsored by:

11th & 12th Grade - January 26, 2008 Individual Multiple Choice Contest

1	Evaluate: (1	og ₃ 128)(log ₂ 24:	3)		
	A) 35	B) 42	C) 12	D) 36	E) NOTA
2	What is the	sum of the r	oots of the f	ollowing func	tion? $x^2 - 56x + 71 = 0$
	A) -23		C) 56	D) 71	
3	Evaluate in				
	10100 10111	11102			
	+101110				
	A) 211231 ₄	B) 120231 ₄	C) 121211 ₄	D) 130211 ₄	F) NOTA
4	•	•	•		mplify. What is the resulting
•	Narionanzo	THE GOLDHAM		_	mpn, y. what is the resulting
	denominator	r?	$\frac{\sqrt{5}}{5-\sqrt{2}}$		
			5 – √2	! – √3	
	A)41	B) 94	C) 122	D) 180	E) NOTA
5		$3^{27^x} = 27^{3^x}$			
		B) 1/3	C) 1/2	D) 1	E) NOTA
6	Eliminate th	ne parameter	in the followi	ng parametri	c equations: x = 2t + 5
					y = 4t - 6
	A) y=8t+14	B) x=8t-7	C) y-2x=16	D) 2x-y=16	E) NOTA
7			•		s one side length and triples
				ace area of t	the cube to the surface area of
		tangular prisr		6) 1.27	E) NOTA
0	-	B) 1:5	•	D) 1:36	E) NOTA
8	Solve Lou. X	yz, given that	i		3x + 4y + 2z = 76
					5x - 7y + 3z = -132
					7x + 3y - 5z = 86
	A) 57	B) -114	C) -57	D) 38	
9	How many t	imes does f(x	$x = 3\sin(2x +$	$\frac{\pi}{3}$ -2 inter	E) NOTA rsect the x-axis on the interval
	from 0 to 3		•	. •	
	A) 2	B) 3	C) 4	D) 5	E) 6

Sponsored by: 9^{th} , 10^{th} , 11^{th} , & 12^{th} Grade - January 26, 2008 Team Contest

1	A circle with a radius of 3 cm rolls around the inside of an equilateral triangle with sides measuring 12 cm. What is the distance, in centimeters, travelled by the center of the circle during one complete circuit?		
2	In $\triangle PQR$, $m\angle P=45^\circ$, $m\angle Q=105^\circ$, and $PQ=6$ cm. What is the length of \overline{QR} , in centimeters?		
3	If set W is the set of all positive multiples of 6 less than 10,000 and set V is the set of all positive perfect squares, how many elements are in the set $V'\cap W$?		
4	My coin collection consists of only nickels, dimes, and quarters, and has a value of \$2.55. If twice the number of nickels is equal to the absolute value of the difference between the number of dimes and the number of quarters, what is the largest number of coins that can be in my collection?		
5	Tony and Albert are setting up a meeting. They decide to meet sometime between 7:00 PM and 8:00 PM. When Tony arrives, he will wait 10 minutes for Albert to show up, then leave if Albert hasn't arrived by then. When Albert arrives, he will wait 5 minutes for Tony to show up, then leave if Tony hasn't arrived by then. If they both arrive at random times between 7:00 and 8:00 PM, what is the probability that they will meet?		
6	The integers from 2 to 10 are each put in a cell of a 3x3 magic square so that each cell receives a number. If each row, column, and diagonal has the same sum, what is the sum of s, t, and u? $\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
7	The Clymer test detects MIC syndrome, which affects one person in a million. A person with MIC will test positive 99% of the time and a person without it will test negative 97% of the time. What is the probability that you have MIC if you test positive for it using the Clymer test?		
8	In an old-fashioned mill, eight horses walking for nine hours can grind 300 kg of flour. How many minutes, would it take six horses to grind 120 kg of flour?		
9	Let n be a natural number whose square is greater than 100 and less than 300. Find the sum of all possible values of n , given that ${}_{n}\mathcal{C}_{n-10}$ is not a palindrome. (A palindrome is a number that remains the same when its digits are reversed. The notation ${}_{n}\mathcal{C}_{k}$ indicates the number of ways to choose k objects from a set of n distinct objects, without regard to order.)		
10	What is the area of the triangle with vertices at the points $(4,-1)$, $(-2,5)$, and $(-3,-3)$?		

Sponsored by:

11th & 12th Grade - January 26, 2008 Pressure Round Contest

1	Put the following 6 values in order from least to greatest. Your answer should consist of 6 letters in the correct order. $A=999$ $B=9^{99}$ $C=99^9$ $D=9^{99}$ $E=9\cdot 9\cdot 9$ $F=\left(9^9\right)^9$
2	Find the sum of all 3-digit positive integers divisible without remainder by exactly 8 out of 9 single-digit positive integers.
3	A triangle with sides measuring 6, 9, and 12 cm is similar to a triangle with sides measuring 66, 88, and y cm. What is the value of y?
4	175 people stand equally spaced in a circle. They count off consecutively, starting with 1 (1, 2, 3, and so on). The person who says "63" is standing opposite a gap. If the two people next to this gap then leave the circle, what is the sum of the numbers that were called out by all the people still in the circle?
5	Five men and three women sit in a row. In how many ways can they be arranged so that no woman sits next to another woman?

Sponsored by:

11th & 12th Grade - January 26, 2008 Mental Math Contest

PERSO	ON 1	
1.1	Evaluate 63 squared minus 37 squared.	2600
1.2	What is the probability of flipping exactly 4 heads when flipping 7 fair	35
	coins?	128
1.3	What is the sum of the first 6 terms of the geometric sequence	77
	beginning 4, 2, 1 and so on? Express your answer as a mixed number.	8
1.4	What is the sum of the zeros of the equation y equals 117 "x" squared	16
	plus 16 "x" minus 16?	117
PERSO	ON 2	
2.1	What is the area of the triangle bounded by the zeros and vertex of	64 [un ²]
	the function y equals "x" squared minus eight "x"?	
2.2	Find the sum of the first hundred even natural numbers.	10100
2.3	Evaluate 216 to the negative two-thirds power.	1/36
2.4	The cosine of a fourth-quadrant angle is seven-ninths, what is its sine?	$4\sqrt{2}$
		9
PERSO	ON 3	
3.1	Find the least common multiple of 187 and 68.	748
3.2	What is the perimeter of a rhombus with sides measuring 23	92 [cm]
	centimeters?	
3.3	What is the area of a triangle with sides of length 4, 5, and 7?	$4\sqrt{6} \text{ [un}^2\text{]}$
3.4	What is the slope of the line tangent to the circle "x" squared plus "y"	$\sqrt{3}$
	squared equals one at the point negative one half root 3 comma one	, -
	half?	
PERSO	DN 4	
4.1	What value of "X" satisfies the equation three "X" minus four equals	14
	thirty-eight?	
4.2	How many seating arrangements are possible in a small classroom with	720
	6 chairs in a line, but only 5 students?	[arrangements]
4.3	What is the sum of the first 10 perfect squares?	385
4.4	I want to meet with my friend in Mexico. We decide that we will both	7
	go to our favorite city during the 2008 calendar year and will stay for	16
	3 months and then leave. What is the probability that we will be in our	
	favorite city at the same time?	

Sponsored by:

11th & 12th Grade - January 26, 2008

COLLEGE KNOWLEDGE BOWL ROUND #1

1 Find the distance between the point 15 comma 8 and the line Y equals three X plus eight. 2 Evaluate: the log base five of eight times the log base two of twenty-five. 3 Cam, Joel and Trevor are mowing the lawn. It takes Cam 2 hours to mow the lawn by himself and it takes Joel 90 minutes. If it takes the three of them working together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? 4 Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. 5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed 8 Find the sum of the four non-real fifth roots of 1. -1	#	Problem	Answer
Evaluate: the log base five of eight times the log base two of twenty-five. 3	1	Find the distance between the point 15 comma 8 and	
two of twenty-five. 3 Cam, Joel and Trevor are mowing the lawn. It takes Cam 2 hours to mow the lawn by himself and it takes Joel 90 minutes. If it takes the three of them working together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? 4 Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. 5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		the line Y equals three X plus eight.	2
 Cam, Joel and Trevor are mowing the lawn. It takes Cam 2 hours to mow the lawn by himself and it takes Joel 90 minutes. If it takes the three of them working together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed 	2	Evaluate: the log base five of eight times the log base	6
Cam 2 hours to mow the lawn by himself and it takes Joel 90 minutes. If it takes the three of them working together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. Tif the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		two of twenty-five.	
Joel 90 minutes. If it takes the three of them working together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. Tif the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed	3	Cam, Joel and Trevor are mowing the lawn. It takes	6 [hours]
together 45 minutes, how long does it take Trevor to mow the lawn by himself, in hours? Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. The sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		Cam 2 hours to mow the lawn by himself and it takes	
mow the lawn by himself, in hours? Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. The sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		Joel 90 minutes. If it takes the three of them working	
 Two of the sides of a triangle have length 20 and the square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed 		together 45 minutes, how long does it take Trevor to	
square root of 3. The angle between the two measures 30 degrees. Find the length of the side opposite this angle. 5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		mow the lawn by himself, in hours?	
30 degrees. Find the length of the side opposite this angle. 5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed	4	Two of the sides of a triangle have length 20 and the	7√7 [un]
angle. 5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		square root of 3. The angle between the two measures	
5 A cube is inscribed in a sphere with volume 36 pi. Find the surface area of the cube. 6 The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		30 degrees. Find the length of the side opposite this	
the surface area of the cube. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus K. The parabola given by the equation Y equals the quantity Two X plus eight has vertex with coordinates H comma K. Find H plus eight has vertex with coordinates H comma K. Find H plus eight has vertex eight has verte		angle.	
The parabola given by the equation Y equals the quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. The sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed	5	A cube is inscribed in a sphere with volume 36 pi. Find	72 [un]
quantity X minus three times the quantity two X plus eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		the surface area of the cube.	
eight has vertex with coordinates H comma K. Find H plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed	6	The parabola given by the equation Y equals the	-25
plus K. 7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		quantity X minus three times the quantity two X plus	
7 If the sum of the squares of X and Y is 11 and the product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		eight has vertex with coordinates H comma K. Find H	
product of X and Y is 7, find the absolute value of the sum of X and Y, times two. Extra Problem - Only if Needed		plus K.	
sum of X and Y, times two. Extra Problem - Only if Needed	7	If the sum of the squares of X and Y is 11 and the	10
Extra Problem - Only if Needed		product of X and Y is 7, find the absolute value of the	
· · · · · · · · · · · · · · · · · · ·		sum of X and Y , times two.	
· · · · · · · · · · · · · · · · · · ·		Extra Problem – Only if Needed	
	8	•	-1

Sponsored by:

11th & 12th Grade - January 26, 2008

COLLEGE KNOWLEDGE BOWL ROUND #2

#	Problem	Answer
1	Two circles with radii of lengths 24 and 1 are	4√6 [un]
	tangent to each other. What is the length of the	
	external tangent connecting the two circles?	
2	What is the probability of drawing an ace, king or	19
	diamond from a standard deck of 52 cards?	52
3	What is the length of the altitude to the	168 [un]
	hypotenuse of a right triangle with legs of length 7	25 []
	and 24?	
4	Find the remainder when 3 to the 18th power is	4
	divided by 5.	
5	When X equals one-half, what is the sum of the	4
	infinite series 1 plus 2 "X" plus 3 "X"-squared plus 4	
	"X"-cubed and so forth?	
6	How many two letter permutations can be made	13
	from the letters B O O T H?	
7	Find the area of the shape described by the	8π [un ²]
	equation four X squared minus twenty-four X plus	
	Y squared minus four Y plus twenty-four equals	
	zero.	
	Extra Problem - Only if Needed	
8	Evaluate the quantity tangent squared of 15 degrees [PAUSE]	1
	plus one times the quantity sine squared of 105 degrees.	

Sponsored by:

11th & 12th Grade - January 26, 2008

COLLEGE KNOWLEDGE BOWL ROUND #3

#	Problem	Answer
1	Find the coefficient of the X squared term in the expansion of X squared plus the quantity 3 over X, quantity to the seventh power.	2835
2	On the interval from 0 to 2 pi, how many solutions for "X" are there for which the sine of 2 "X" equals the cosine of "X"?	4
3	What is the radius of the circle inscribed in a triangle with side lengths of 3, 4 and 5?	1 [un]
4	How many different ways can you hand out 9 pinecones to 4 people if each person must receive at least 1 pinecone?	56 [ways]
5	Find the sum of the roots minus the product of the roots of the equation: the quantity X squared plus nine times the quantity X squared minus X plus ten equals zero.	-89
6	What is the speed of a ball when it hits the ground if the height is given by the function h of t equals 64 - 16 t-squared?	64 or -64
7	What is the distance between the line described by 3 "Y" equals 4 "X" plus 1 and the line 3 "Y" equals 4 "X" plus 4?	3/5
	Extra Problem - Only if Needed	
8	An airplane is flying north at 100 miles per hour, its maximum speed. At this rate, it uses 1 gallon of fuel per hour. It encounters a 10 root 2 mile per hour head wind coming from directly northeast. If it has 2 gallons of fuel left, how far will it travel, assuming the pilot maintains maximum speed?	20√82 [miles]



11th & 12th Grade - January 26, 2008

School Name	I eam #	
Proctor Name	Room #	First Score
STUDENT NAME		(out of 18)

INDIVIDUAL MULTIPLE CHOICE - 15 minutes

This test is the only test where you will be penalized for incorrect responses. You will receive 2 points for a correct letter response, 0 points for leaving it blank and -1 point for an incorrect response. It is not necessary to write your personal name on the test, but you may put it at the bottom of the test so your coach will be able to give you back the correct test. This test is taken individually, but it is part of your team score, including zeros for missing team members. Your team score will be calculated by taking the mean of your four team members' scores. When you are prompted to begin, tear off the colored sheet and begin testing. Since this is a multiple choice test, ONLY a letter response should be indicated as an answer on the answer sheet. No talking during the test.

DO NOT WRITE IN SHADED REGIONS

	Answer	-1, 0 or 2	-1, 0 or 2
1	A		
2	С		
3	D		
4	В		
5	С		
6	D		
7	С		
8	В		
9	E(6)		



11th & 12th Grade - January 26, 2008

School Name	Team #	
Proctor Name	Room #	First Score
STUDENT NAME		(out of 20)

Team Contest - Score Sheet

TEAM TEST - 15 minutes

When you are prompted to begin, tear off the colored sheet and give a copy of the test to each of your team members and begin testing. Each problem is scored as **2 or 0**. Record all answers on the colored answer sheet.

DO NOT WRITE IN SHADED REGIONS

	Answer	2 or 0	2 or 0
1	36 – 18√3 [cm]		
2	6√2 [cm]		
3	1650 [elements]		
4	24 [coins]		
5	67 288		
6	27		
7	1/30304		
8	288 [min]		
9	30		
10	27 [un ²]		

"Math is Cool" Masters - 2007-08 11th & 12th Grade - January 26, 2008



School Name	Team #
Proctor Name	Room #
STUDENT NAME	

PRESSURE ROUND - 10 minutes

When it is time to begin, you will be handed a packet of questions. There is a copy of the questions for each team member. Two minutes after the start of the test you are expected to submit an answer for one of the questions (it can simply be a guess). The maximum value of this answer is 1 point. In another two minutes you are expected to submit another answer to one of the four remaining questions; its maximum value is two points. This process will continue until all the questions are answered and each consecutive question's worth will go up by one point. You must submit your answers on the colored sheets given to you. If you do not have an answer at the end of a two minute period, you must still submit an answer sheet with an identified question number on it. Failure to do so will result in loss of points. This event is timed, and you will be given a verbal 5 second warning and told to hold your answer sheet up in the air. You may keep working as the sheets are collected.

Pressure Round Answers

Answer	
1	EACFBD [in order]
2	2424
3	44
4	15,099
5	14,400 [ways]