December 1, 2012 7th & 8th Grade Mental Math Contest

Follow along as your proctor reads these instructions to you. Your Mental Math score sheet is on the back.

GENERAL INSTRUCTIONS applying to all tests:

- Good sportsmanship is expected throughout the competition by <u>all</u> involved, both competitors and observers. Display of poor sportsmanship may result in disqualification.
- Calculators or any other aids may not be used on any portion of this contest.
- Unless stated otherwise, all rational, non-integer answers need to be expressed as reduced common fractions except in case of problems dealing with money. In the case of problems requiring dollar answers, answer as a decimal rounded to the nearest hundredth (ie, to the nearest cent).
- All radicals must be simplified and all denominators must be rationalized.
- Units are not necessary as part of your answer unless it is a problem that deals with time and in that case, a.m. or p.m. is required. However, if you choose to use units, they must be correct.
- Leave all answers in terms of π where applicable.
- Do not round any answers unless stated otherwise.
- Record all answers on the colored cover sheets in the answer column only.
- Make sure all answer sheets have all the information (name, team number, etc.) at the top of the sheet filled out.
- Tests will be scored as a 0 if answers are not recorded on the answer sheets.
- Blank answer sheets and answer sheets with no name will be scored as a 0.

Mental Math - 30 sec per question

8 problems read orally to everyone - Approximately 8% of Individual Score - 25% of team score

When it is time to begin, the proctor will read the first question twice. You may not do any writing or talking while arriving at a solution. Once you have a solution, record it on the sheet in front of you. You may not change or cross out answers once you have written an answer down. If there are eraser marks, write-overs, or crossed-out answers, they will be marked wrong. Once all students have laid their pencils on the desk, another question will be asked. If a student doesn't lay his/her pencil down, the maximum wait time is 30 seconds after completion of the second reading of the question before another question is asked. You may continue to work on a problem while the next question is being read. The value of each question is a one or zero. Each student will be asked the same eight questions. Individual scores used to determine individual placing will be determined by the sum of the Mental Math score and the Individual Test score for each individual. In addition, the top three Mental Math scores from one team will be totaled and doubled and will contribute to 25% of the team score.

7th & 8th Grade - December 1, 2012 Mental Math Contest

Mental Math - 30 sec per question

8 problems read orally to everyone - Approximately 8% of Individual Score - 25% of team score

When it is time to begin, the proctor will read the first question twice. You may not do any writing or talking while arriving at a solution. Once you have a solution, record it on the sheet in front of you. You may not change or cross out answers once you have written an answer down. If there are eraser marks, write-overs, or crossed-out answers, they will be marked wrong. Once all students have laid their pencils on the desk, another question will be asked. If a student doesn't lay his/her pencil down, the maximum wait time is 30 seconds after completion of the second reading of the question before another question is asked. You may continue to work on a problem while the next question is being read. The value of each question is a one or zero. Each student will be asked the same eight questions. Individual scores used to determine individual placing will be determined by the sum of the Mental Math score and the Individual Test score for each individual. In addition, the top three Mental Math scores from one team will be totaled and doubled and will contribute to 25% of the team score.

#	Problem
1	There are fourteen banana boats. Each banana boat carries sixty-four bananas. If six banana boats get attacked by crocodiles and lose their bananas, how many bananas are left?
2	A palindrome is a counting number that looks the same when you reverse its digits. How many palindromes are between ten and one hundred five?
3	How many square inches of paper would it take to cover the side of a five-inch tall cylindrical soup can having a three-inch radius?
4	If the product of two numbers is ninety-six, and their sum is twenty, what is the greatest common factor of those two numbers?
5	Martha is facing north. If she then turns ninety degrees clockwise, then one hundred eighty degrees clockwise, then two hundred seventy degrees clockwise, which direction would Martha be facing?
6	If I am awake for twelve hours, and spend twenty-five percent of my waking hours listening to music, what is the probability in a percentage that I will not be listening to music during the twelve hours I am awake?
7	What is the second largest three-digit number with three distinct digits that are all prime numbers?
8	A regular hexagon has nine diagonals. How many of these diagonals are parallel to at least one of the sides of the hexagon?

December 1, 2012 Algebra Individual Contest

Tear this cover sheet and scratch paper off and fill out the top of the colored answer sheet prior to the start of the test. The graph below is for your use, if needed.

INDIVIDUAL TEST - ALGEBRA - 35 minutes

You may NOT be seated next to anyone from your school. If you are MOVE NOW to avoid being disqualified! When you are prompted to begin, tear off the colored sheet and begin testing. Make sure your name and school are recorded on the answer sheet. The raw score will be 2 points for correct answers to problems 1-30 and 3 points for 31-40. Record your answers on the score sheet. No talking during the test. You will be given a 5 minute time warning.

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December 1, 2012 Algebra Individual Contest

	Questions 1-30: 2 points each
1	What is the positive difference between the greatest three digit number and the greatest one digit number?
2	How many odd numbers are there between 22 and 44?
3	What is the least common multiple of 3, 5, and 11?
4	What is the quotient of 3 ⁷ divided by 3 ⁵ ?
5	How many integers are in the following arithmetic sequence: 0, 1, 2, , 83, 84, 85?
6	Simplify the following expression by combining like terms: -4 + a - 2b + 4a - b + 7
7	Evaluate: $\frac{1+2+3+4++100}{2+4+6+8++200}$
8	How many quadrants does the graph of y=12x+3 go through?
9	Solve for x: $5^x = 625$
10	Rewrite the following expression in expanded form: 4(2a + 3)
11	A tank is half full of water. When 5 gallons of water are added, the tank is three-fourths full. What is the maximum number of gallons the tank can hold?
12	What is the greatest common factor of all prime numbers between 10 and 20?
13	Suhmiin has chosen the first four digits of a 5-digit number in such a way that it is possible to make it a palindrome. How many different digits could she pick to complete this 5-digit palindrome?
14	Tyson, Sabrina, James and Jayze visit some historic sites in Boston. Sabrina goes to 5 sites, Tyson goes to 1 site, James goes to 4 sites and Jayze goes to 2 sites. If Sabrina and James go to 3 sites together, and otherwise each person visits sites that are different from those visited by the other three, how many different sites are visited?
15	Two congruent circles are positioned on a plane so that their centers are 12 cm apart. What must the number of centimeters in the radius of each circle be in order for them to be externally tangent?
16	When an entire math class stands equally spaced in a circle, student number 4 is directly opposite student number 12. If fourteen students leave to attend a math competition, how many students are left in the class?
17	A rectangle has integer side lengths and an area of 72 square inches. In inches, what is the largest possible perimeter of this rectangle?

18	What is the x-coordinate of the point of intersection of the two lines represented by the following
-0	two equations? 7x + 2y = 9
	5x - 4y = 1
10	Each of the variables a, b, c, d, e, and f represent one of the integers in the set {-4, -2, 0, 2, 4, 6},
19	not necessarily in that order. What is the greatest possible value of $\frac{a}{b} + \frac{c}{d} + \frac{e}{f}$?
20	The shape below is a trapezoid and the segment labeled $6x - 18$ is its median. What is the value of x ?
	5x + 7
	6x - 18
	0X - 10
	3x+1
	James is walking in a square path starting at a corner. He walks around the path once and then
21	walks directly to the corner farthest away from him. What is the number of meters in the total
	distance he walks if the square has a diagonal of length of $24\sqrt{2}$ meters?
22	A fish has three parts: head, midsection, and tail. A fish's tail is approximately half of the length
22	from its head to the end of its midsection. Its head is approximately one-third of its midsection
	length. If the fish's head is an inch long, how many inches long is the entire fish?
23	A construction worker is filling a trough with cement. The trough is a rectangular prism 18 feet
50	long, 9 feet wide, and 3 feet deep. How many cubic yards of cement must the construction worker pour?
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24	Find the median of the following set of five values: $\sqrt{8}$, $2^{\frac{-1}{3}}$, $9^{\frac{2}{3}}$, $\sqrt[3]{6}$, $\frac{1}{\sqrt{3}}$
25	What is the sum of the infinite geometric series that starts with one-third and has a common ratio
	of one-fourth?
26	Two horses are racing around a 1-mile track. Horse A runs at 30 mph the entire time. If horse B
-•	runs at 20 mph on the first quarter of the track, at what speed, in miles per hour, will horse B need to run on the rest of the track to tie horse A?
~7	Solve the equation for y.
27	$\frac{y-2}{2} = \frac{3}{4} + \frac{7-3y}{8}$
28	A perfect number is a number where all of its factors, excluding the number itself, sum to the
20	number itself. One formula for generating perfect numbers is $2^{p-1}(2^p-1)$ where p and $2^p - 1$ both
	represent prime numbers. What is the fourth largest perfect number?
29	What is the probability that three cards selected randomly from a standard deck of cards, without
-/	replacement, are all odd integers? For example, one possible set of three odd integer cards includes 3 of hearts, 3 of diamonds, and 3 of spades. Ace, Jack, and King are not odd integers.
	How many ways can $\sqrt{108}$ be written in the form $a\sqrt{b}$, where a and b are integers, b < 108, and b has
30	no perfect square factors greater than 36?
	no per reci square ruciors greater mun sor

	Challenge Questions: 3 pts each
31	What is the height in centimeters of an equilateral triangle whose perimeter is $6\sqrt{2}$ cm?
32	Anna bets \$100 on a game. There are three possible outcomes of her bet. There is a 4/10 probability that she will get her money back and a 50% chance that she will lose her \$100. Otherwise she will get her money back plus \$50. How many dollars, on average, will Anna gain or lose if she bets \$100? Your answer should be positive if she gains, and negative if she loses.
33	In the 4 by 5 array of dots, how many non-square rectangles can be drawn
34	The speed of light is 3 x 10 ⁸ meters per second. If Jupiter is 2.25 x 10 ²⁵ meters from the sun, how many seconds does it take light to reach Jupiter from the sun? Answer in scientific notation. D, E, F, and G are the midpoints of the sides of square PQRS. Find the area of the shaded region,
35	in square centimeters, given that the perimeter of the outer square is 40 cm. P = P = P = P = P = P = P = P = P = P =
36	The numbers $1\frac{1}{2}$ and $5\frac{1}{16}$ are terms three and six of the geometric sequence having $\frac{2}{3}$ as term one. What is the positive difference between terms four and five? Answer as a common fraction.
37	A data set with six distinct positive integers has a mean of 26 and a median of 23. If the numbers are listed in order from least to greatest, what is the largest possible value of the 5 th term?
38	There is a point (5, 7). Reflect the point across the line with equation $y = \frac{1}{2}x - \frac{7}{4}$. As an ordered pair (x, y), what are the coordinates of the reflected point?
39	Write an equation in the form $y = ax^2 + bx + c$ for which each (x, y) pair in the following table is a solution. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
40	In base ten, find the sum of the first fifteen terms of the following sequence: $10_2, 21_3, 32_4, 43_5, 54_6, 65_7, 76_8, 87_9, 98_{10}, \dots$

December 1, 2012 GEOMETRY Individual Contest

Tear this cover sheet and scratch paper off and fill out the top of the colored answer sheet prior to the start of the test. The graph below is for your use, if needed.

INDIVIDUAL TEST - GEOMETRY - 35 minutes

You may NOT be seated next to anyone from your school. If you are MOVE NOW to avoid being disqualified! When you are prompted to begin, tear off the colored sheet and begin testing. Make sure your name and school are recorded on the answer sheet. The raw score will be 2 points for correct answers to problems 1-30 and 3 points for 31-40. Record your answers on the score sheet. No talking during the test. You will be given a 5 minute time warning.

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December 1, 2012 Geometry Individual Contest

	Questions 1-30: 2 points each
1	How many integers are in the following arithmetic sequence: 0, 1, 2, , 83, 84, 85?
2	Simplify the following expression by combining like terms: -4 + a - 2b + 4a - b + 7
3	An ant is on the search for food. It travels 4 feet north, 3 feet east and one foot south from its home when it comes upon a cache of food. As a simplified radical, what is the least number of feet the ant could travel to get back home?
4	Evaluate: $\frac{1+2+3+4++100}{2+4+6+8++200}$
5	A note pad is made of identical sheets of paper having a density of 1.5 grams per cubic centimeter. If the pad is 4 cm high, 7 cm wide, and 16 cm long, what is its weight in grams?
6	How many quadrants does the graph of y=12x+3 go through?
7	When the five diagonals of a regular pentagon are drawn, how many non-overlapping regions within the pentagon are created?
8	The area of $\triangle ABC$ is 240 ft ² . In square feet, what is the area of $\triangle ABD$? Note: Image is not to scale. B 10 D 20 C
9	Rewrite the following expression in expanded form: 4(2a + 3)
10	Two congruent circles are positioned on a plane so that their centers are 12 cm apart. What must the number of centimeters in the radius of each circle be in order for them to be externally tangent?
11	A tank is half full of water. When 5 gallons of water are added, the tank is three-fourths full. What is the maximum number of gallons the tank can hold?
12	The shape below is a trapezoid and the segment labeled $6x - 18$ is its median. What is the value of x? $5x + 7$ 6x - 18 3x + 1

13	Suhmiin has chosen the first four digits of a 5-digit number in such a way that it is possible to
12	make it a palindrome. How many different digits could she pick to complete this 5-digit palindrome?
14	A rectangle has integer side lengths and an area of 72 square inches. In inches, what is the largest
T-	possible perimeter of this rectangle?
15	Solve the equation for y.
15	$\frac{y-2}{2} = \frac{3}{4} + \frac{7-3y}{8}$
16	When an entire math class stands equally spaced in a circle, student number 4 is directly opposite
10	student number 12. If fourteen students leave to attend a math competition, how many students
	are left in the class?
17	A fish has three parts: head, midsection, and tail. A fish's tail is approximately half of the length
1/	from its head to the end of its midsection. Its head is approximately one-third of its midsection
	length. If the fish's head is an inch long, how many inches long is the entire fish?
18	What is the x-coordinate of the point of intersection of the two lines represented by the following
10	two equations?
	7x + 2y = 9
	5x - 4y = 1
19	Each of the variables a, b, c, d, e, and f represent one of the integers in the set {-4, -2, 0, 2, 4, 6},
	not necessarily in that order. What is the greatest possible value of $\frac{a}{b} + \frac{c}{d} + \frac{e}{f}$?
20	A perfect number is a number where all of its factors, excluding the number itself, sum to the
20	number itself. One formula for generating perfect numbers is $2^{p-1}(2^p-1)$ where p and 2^p-1 both
	represent prime numbers. What is the fourth largest perfect number?
21	James is walking in a square path starting at a corner. He walks around the path once and then
21	walks directly to the corner farthest away from him. What is the number of meters in the total
	distance he walks if the square has a diagonal of length of $24\sqrt{2}$ meters?
22	What is the number of centimeters in the semi-perimeter of a right triangle with one leg 3 cm and
	hypotenuse 5 cm?
23	A construction worker is filling a trough with cement. The trough is a rectangular prism 18 feet
23	long, 9 feet wide, and 3 feet deep. How many cubic yards of cement must the construction worker
	pour?
24	Find the median of the following set of five values: $\sqrt{8}$, $2^{\frac{-1}{3}}$, $9^{\frac{2}{3}}$, $\sqrt[3]{6}$, $\frac{1}{\sqrt{3}}$
51	The method of the following set of the values: $\sqrt{3}$, $\sqrt{3}$
25	Quadrilateral ABCD has vertices A(3,2), B(2,7), C(4,7), and D(5,2). In square units, what is the area
25	of ABCD?
26	Two horses are racing around a 1-mile track. Horse A runs at 30 mph the entire time. If horse B
20	runs at 20 mph on the first quarter of the track, at what speed, in miles per hour, will horse B need
	to run on the rest of the track to tie horse A?
27	What is the length in meters of the space diagonal of a cube with side length 4 m?
28	What is the probability that three cards selected randomly from a standard deck of cards, without
	replacement, are all odd integers? For example, one possible set of three odd integer cards
	includes 3 of hearts, 3 of diamonds, and 3 of spades. Ace, Jack, and King are not odd integers.
29	How many ways can $\sqrt{108}$ be written in the form $a\sqrt{b}$, where a and b are integers, b < 108, and b has
	no perfect square factors greater than 36?
30	What is the height in centimeters of an equilateral triangle whose perimeter is $6\sqrt{2}$ cm?

	Challenge Questions: 3 pts each
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33	The speed of light is 3 x 10^8 meters per second. If Jupiter is 2.25 x 10^{25} meters from the sun, how many seconds does it take light to reach Jupiter from the sun? Answer in scientific notation.
34	<i>D, E, F,</i> and <i>G</i> are the midpoints of the sides of square <i>PQRS</i> . Find the area of the shaded region, in square centimeters, given that the perimeter of the outer square is 40 cm.
	$P \qquad F \qquad Q$ $G \qquad E$ $G \qquad D \qquad R$
35	The numbers $1\frac{1}{2}$ and $5\frac{1}{16}$ are terms three and six of the geometric sequence having $\frac{2}{3}$ as term one. What is the positive difference between terms four and five? Answer as a common fraction.
36	A data set with six distinct positive integers has a mean of 26 and a median of 23. If the numbers are listed in order from least to greatest, what is the largest possible value of the 5 th term?
37	There is a point (5, 7). Reflect the point across the line with equation $y = \frac{1}{2}x - \frac{7}{4}$. As an ordered pair (x, y), what are the coordinates of the reflected point?
38	pair (x, y), what are the coordinates of the reflected point? Two 2-inch by 2-inch squares are sitting on top of each other. One square is rotated 45° to create the shown picture. What is the area of the shaded region, in square inches?

Write an equation in the form $y = ax^2 + bx + c$ for which each (x, y) pair in the following table is a											
$39 \begin{bmatrix} write an equation in the form y = dx + bx + c for which each (x, y) pair in the following table is solution.\boxed{x -4 -2 \ 0 \ 1 \ 2 \ 3}$											
y -18 14 30 32 30 24											
40 In base ten, find the sum of the first fifteen terms of the following sequence: $10_2, 21_3, 32_4, 43_5, 54_6, 65_7, 76_8, 87_9, 98_{10}, \dots$											

8th Grade - December 1, 2012 Individual Multiple Choice Contest

	USE THE FOLLOWING TABLE FOR PROBLEMS 1-3							
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	•			•	• •	ring from 1 to 4 line		
	throug			I		5.0		
		Level	Points for 1 line cleared	Points for 2 lines cleared	Points for 3 lines cleared	Points for 4 lines cleared		
		0	40	at once	at once	at once		
		0	40 80	100 200	300 600	1200 2400		
		2	120	300	900	3600		
		9	400	1000	3000	12000		
		n	40 <i>(n+1)</i>	100 <i>(n+1)</i>	300 <i>(n+1)</i>	1200 <i>(n+1)</i>		
1	At lev line?	el O, how	many times mor	e points do you	get for clearing	4 lines at once, the	an for clearing 1	
	A) 3		B) 30	C) 300	D) 1160 E)	Answer not given.		
2		•			•	that can be earned	d for clearing 3	
2			level 9 and for	-				
	A) 180	00	B) 600	<i>C</i>) 0	D)-600 E)	Answer not given.		
3		length of		•		init long. What is th tely inside one of t		
	A) 2√	$\overline{2}$	B) √10	C) √13	D) √17 E)	Answer not given.		
	1							

	USE THE FOLLOWING SCENARIO AND GRAPH FOR PROBLEMS 4-6 Betty's Fence Project
	Betty wants to build a fence to enclose a rectangular section of her back yard. She has 60 ft of fencing material and her house will serve as one of the walls of the rectangle. The following graph shows possible areas of the rectangle as a function of the width of the rectangle. The equation for the graph is $y = x(60-2x)$.
4	When the width of the rectangle is 10 feet, the area is 400 ft^2 . At what other width will the area also be 400 ft^2 ?
	A) 21 ft B) 20 ft C) 19.5 ft D) 19 ft E) Answer not given.
5	If the equation for this graph is written in the form $y = ax^2 + bx + c$ then what is the value of a + b
J	$+ c^{2}$
	A) 32B) 56C) 60D) 64E) Answer not given.If the width must be a positive even integer, what is the mean of all possible positive areas of the
6	rectangle?
	A) 450 ft^2 B) 400 ft^2 C) 360 ft^2 D) 320 ft^2 E) Answer not given.
	USE THE FOLLOWING LIST FOR PROBLEMS 7-10.
	360 is the smallest positive integer to have exactly 24 factors. These 24 factors are listed as follows in the form 2^{a} 2^{b} 5^{c} . The first column has the smallest six factors of 360 in second inc
	follows in the form $2^a \cdot 3^b \cdot 5^c$. The first column has the smallest six factors of 360 in ascending order, the second column has the 7 th through 12 th largest factors in ascending order, and so on with
	the largest factor of 360 at the bottom of the fourth column. For example, $2^0 \cdot 3^0 \cdot 5^0$ is the
	smallest factor of 24 and it equals 1, while $2^3 \cdot 3^2 \cdot 5^1$ is the largest factor of 360 and it equals 360.
	$2^0 \cdot 3^0 \cdot 5^0$ $2^3 \cdot 3^0 \cdot 5^0$ $2^2 \cdot 3^0 \cdot 5^1$ $2^2 \cdot 3^1 \cdot 5^1$
	$2^1 \cdot 3^0 \cdot 5^0$ $2^0 \cdot 3^2 \cdot 5^0$ $2^3 \cdot 3^1 \cdot 5^0$ $2^3 \cdot 3^2 \cdot 5^0$
	$2^0 \cdot 3^1 \cdot 5^0$ $2^1 \cdot 3^0 \cdot 5^1$ $2^1 \cdot 3^1 \cdot 5^1$ $2^1 \cdot 3^2 \cdot 5^1$
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	$2^{1} \cdot 3^{1} \cdot 5^{0} \qquad 2^{1} \cdot 3^{2} \cdot 5^{0} \qquad 2^{0} \cdot 3^{2} \cdot 5^{1} \qquad 2^{3} \cdot 3^{2} \cdot 5^{1}$
7	How many of the factors of 360 are odd? A) 6 B) 12 C) 18 D) 24 E) Answer not given.
8	What is the sustion of the 2 nd langest featon divided by the 2 nd smallest featon of 2402
	What is the quotient of the 2 nd largest factor divided by the 2 nd smallest factor of 360?A) 180B) 150C) 120D) 90E) Answer not given.
9	
	A) 180B) 150C) 120D) 90E) Answer not given.What positive integer less than 1000 has exactly 24 factors and is not a multiple of 30?

8th Grade – December 1, 2012 Team Contest

1	When the number of minutes in a year is expressed in scientific notation, what is the exponent of 10?
2	What number must you multiply by 28 to get the same result as the square of 35? If your answer is not a whole number, give it as a reduced fraction.
3	What is the smallest counting number that could be added to 2012 so that the sum is a multiple of 7?
4	A cube has a surface area of 54 square inches. If the surface area of the cube is increased <u>by</u> 300%, what is the volume of the new cube, in cubic inches?
5	The minute hand of a clock has traveled 2012 degrees since 7:40 PM. To the nearest second, what time is it? Give your answer in the form "hr : min : sec", and include "AM " or "PM".
6	The ratio of 7 th graders to 8 th graders at a Math Is Cool contest was 11 to 8. If there were at least 300 students at the contest (all in grade 7 or grade 8), what is the smallest number of 7 th graders who could have participated?
7	In a Fibonacci sequence, each term after the first two terms is the sum of the two previous terms. In a Tribonacci sequence, each term after the first three terms is the sum of the three previous terms. Let F_n be the nth term of a Fibonacci sequence
	whose first two terms are {1, 1}, and T_n be the nth term of a Tribonacci sequence whose first three terms are {0, 1, 1}. For what value or values of n does $F_n = T_n$?
8	A lucky number is any counting number with two or more digits the same. For example, "33", "828 ", and "777" are all lucky numbers. How many lucky numbers are there less than 1000?
9	A regular tetrahedron is inscribed in a sphere. If the side length of the tetrahedron is 12 centimeters, what is the radius of the sphere, in centimeters?
10	A special die (number cube) is weighted so that the probability of rolling <i>n</i> on one roll of the die is exactly $\frac{1}{n}$ for each of the six values of <i>n</i> . The numbers on five of the faces of this die are 6, 3, 18, 4, and 12. As a reduced fraction, what is the
	probability that the product of two rolls of this die will be 36?

8th Grade - December 1, 2012 Pressure Round Contest

1	Brian has a deck of cards with integer values from 1 through 5. There are four cards of each value (i.e. four 1's, four 2's, etc.). If Brian draws three cards at random without replacement, what is the probability that the sum of the values of the three cards will be a prime number?
2	If seven liters of a 25% acid solution are mixed with three liters of a 25% acid solution, and then two and a half liters of water are added, what percentage of the resultant mixture is acid?
3	The apothem of a regular polygon is a segment drawn from the center of the polygon perpendicular to and intersecting at the midpoint of one of the sides of the polygon. Find the area of a regular polygon with apothem of 7 and perimeter of 18.
4	The figure shown has two concentric circles of radius 10 cm and 8 cm and the area between them is shaded. The edges of the wide shaded strip across the middle are parallel. AB is 8 cm and the midpoint of segment AB is at the center of the circles. Find the area, in square centimeters, of the shaded region.
5	Today's date, when written in the form ab/ab/ab, is 12/01/12. It has one 0, two 2s, and three 1s. In how many days will the next date occur which has the same number of 0s, 1s, and 2s, not necessarily in the same order?

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #1 - SET 1

#	Problem	Answer
1	Joe procrastinated and has until ten thirty AM tomorrow to finish	90 [min]
L L	his school project. It is nine PM today when Joe finally starts his	
	project, and he needs twelve hours to finish. What is the maximum	
	number of minutes of sleep that Joe can allow himself if he is to	
	finish his project on time?	
2	Sally has more than twice as many football trading cards as Billy-	39 [trading cards]
2	Bob. Sally has 79 trading cards. What is the greatest number of	
	trading cards Billy-Bob might have?	
2	How many diagonals can be drawn in a heptagon?	14 [diagonals]
3		
Λ	Nine disgruntled turtles have to split a 63-inch long sandwich. What	7 [in]
4	is the number of inches in the length of the part of the sandwich	_
	that each turtle gets if each turtle gets an equal amount?	
F	Two of the turtles decide to steal the 63-inch long sandwich and eat	42 [in.]
5	it from the ends in. Turtle A eats an inch every 10 seconds, and	
	Turtle B eats two inches every 10 seconds. How many inches of	
	sandwich will Turtle B have eaten when the sandwich is gone?	
	The turtle that ate more of the sandwich is too slow to escape the	123 [sec]
6	hungry hawk. If the turtle runs at half a mile per hour and the hawk	
	flies at 30 miles per hour, how long in seconds will it take the hawk	
	to catch the turtle if it is 1 mile away? Round up to the next second.	
_	If every person in a group of 30 people shakes hands exactly once	435 [handshakes]
7	with everyone else in the group, how many handshakes occur?	
-	There are 12 cats. In the fall, those 12 cats each have 3 kittens. In	192 [kittens]
8	the following spring, those 12 original cats and their now-grown	
	kittens have 4 new kittens each. How many new kittens are there?	5774
9	What is 76 times 76?	5776
10	What is the sum of the first 11 prime numbers?	160
IO		

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #2 - SET 2

#	Problem	Answer
1	Robert has 27 shirts and 6 pairs of pants. How many different	162 [outfits]
L	outfits can Robert create?	
2	How many pints are in 14 gallons?	112 [pints]
2		
2	Camiel goes to the pastry shop to buy some sweets. Cupcakes are a	40 [sweets]
3	dollar twenty-five each, cakes are eleven dollars each, and cookies	
	are twenty cents each. If she has twenty dollars and must buy at	
	least 1 of each sweet offered, how many sweets will she buy if she	
	wants to buy the maximum number?	
	What is the 4 th smallest prime number?	7
4		
F	A pack of frosting can cover five sixths of a cookie. As a decimal,	7 point 5 [cookies]
5	how many cookies can be frosted with 9 packs of frosting?	
6	What is 16 squared minus 12 squared?	112
6		
7	Solve the following equation for x: x plus y equals 47 minus y, when y	[x =] 27
7	equals 10.	
0	A triangle has an area of 24 square feet and a height of 10 feet. As	4 point 8 [feet]
8	a decimal, what is the number of feet in the base of the triangle?	
	How many centimeters taller is a cone with a base radius of 2	3 [cm]
9	centimeters and a volume of 6 pi cubic centimeters than a cylinder	
	with a base radius 2 centimeters and a volume of 6 pi cubic	
	centimeters?	
10	In the Fibonacci sequence, terms have the following pattern: one,	798
10	one, two, three, five, eight, thirteen, and so on. In the first 15	
	terms, what is the sum of all terms that are even numbers?	
1	• • • • • • • • • • • • • • • • • • • •	1

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #3 - SET 3

#	Problem	Answer
1	If Jerry runs from the bus stop to school at a rate of 6 miles per hour, and leaves the bus stop at five forty-five AM, what time will he arrive at school if the school is 8 miles away from the bus stop? Include AM or PM.	7:05 AM
2	James has 20 dimes and 15 quarters. Rounding to the nearest whole dollar, how many dollars does James have?	[\$]6
3	Biff and Bo mow the lawn together every week. If Biff can mow the lawn by himself in 30 minutes, and Bo can mow the lawn by himself in 50 minutes, as a decimal to the nearest hundredth, how many minutes will it take them to mow it together?	18 point 75 [minutes]
4	Two bikers are riding next to each other. How much faster is the first biker going, if she is riding at sixty-eight point seven nine miles per hour, and the other is riding at fifty-one point nine two miles per hour?	16 point 87 [mph]
5	On her last 8 tests, Heather earned scores of 61, 72, 60, 77, 84, 80, 90, and 76. She wants an average test score of 77. What does she need to score on her next test?	77
6	What is the y-intercept of the line that is perpendicular to the line with equation 2y equals 3x minus 8 and that passes through the point 3 comma 1? Give your answer as an ordered pair.	zero [comma] three
7	Lacey the dog is on a 5 foot leash attached to the inside corner of two walls. If the supplement of the angle between the walls is 120 degrees, then what is the number of square feet in the area that Lacey can roam?	25 pi over 6 [sq feet] or 25 sixths pi [sq feet]
8	Farmer buys a new ant farm with 250 ants. Each day, two ants hatch and every third day, 2 ants die. How many ants does Farmer have after 4 weeks?	288 [ants]
9	Amber went to the store to buy gardening supplies. When she went to the cashier, she paid ten dollars and sixty-seven cents. If sales tax is 8 percent, to the nearest cent, and in dollars and cents, how much did the tools cost before tax?	9 dollars and 88 cents or 'nine eighty-eight'
10	A trapezoid has an area of 10 square feet and bases whose lengths are integers that differ by two. What is the smallest possible integer number of inches in the height of the trapezoid?	1 [foot]

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #4 - SET 4

#	Problem	Answer
1	If x equals 3, y equals 6, and xyz equals 72, what is the value of z?	4
2	A right isosceles triangle has two sides of length square root of 8 inches. What is the number of inches in the length of the third side?	4 [inches]
3	If a cheetah runs at a rate of 55 miles per hour, how many hours will it take to run 385 miles?	7 [hours]
4	How many letters are in the word Mississippi, if you take out all the "i's"?	7 [letters]
5	The sides of a fair seven-sided die are numbered 1 through 7. Bill rolls it three times. What is the probability that the sum of the three rolls is twenty?	3 over 343 or three three [hundred[and]] forty-thirds
6	Caleb is buying a new car with 3 different sets of tires, 6 paint colors, and 4 headlight types to choose from. If he chooses 1 set of tires, 1 paint color, and 1 type of headlight, in how many ways can he select these features for his car?	72 [ways]
7	How many positive integer factors are there for one thousand two hundred sixty?	36
8	What is 97 times 93?	9021
9	A sphere has a radius of 4 meters. If the radius is increased by 25 percent, how many square meters are in the increase in the sphere's surface area?	36 pi [m ²]
10	How many units from the origin is the vertex of the graph of the function y equals x squared minus 4x plus 11?	square root of 53 [units] or root 53 [units] or radical 53 [units]

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #5 - SET 5

#	Problem	Answer
1	What is the mean of the following set of data: three, six, twenty, sixteen, five	10
2	What is the slope of the line with equation negative 5x plus 6y equals 17?	5 over 6 or five sixths
3	As a common fraction, what is the probability of getting two or three heads when flipping three coins?	1 over 2 or one half
4	Write the repeating decimal, point three nine three nine three nine three nine etcetera as a common fraction.	13 over 33 or thirteen thirty- thirds
5	Bertha eats cake 50 percent faster than Kelsey. Kelsey takes twelve minutes to eat half of the cake, decides she is full, and hands it over to Bertha, who had started eating her own equal- sized cake at the same time Kelsey did. How long does it take her to finish both cakes?	24 [minutes]
6	What is the number of square meters in the surface area of a sphere with diameter 8 meters?	64 pi [m²]
7	What is the number of inches in the perimeter of a regular hexagon with an area of six hundred times the square root of 3 square inches?	120 [in]
8	What is the probability of rolling a standard die and flipping two coins, and getting a 6, a head, and a tail?	1 over 24 or one twenty-fourth
9	What is the number of square inches in the area of a rhombus with diagonals of 10 inches and 8 inches?	40 [square inches]
10	Jeff takes 30 cards and writes the first 30 counting numbers on them, one number per card. He then draws two cards at random, without replacement. As a simplified fraction, what is the probability that both his cards have prime numbers on them?	3 over 29 or three twenty- ninths

8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND #6 - SET 6

#	Problem	Answer
1	Sally rides her bicycle downhill at 60 miles per hour for 30	1 over 2 [mile] or
T	seconds. How many miles did Sally ride downhill?	one half [mile]
2	The Ghostbusters are called twice per day. They catch two	124 [ghosts]
2	ghosts for every call. How many ghosts are caught in January?	_
C	What is the slope of the line that passes through the points	3 over 5 or
3	negative 6 comma 5 and negative 1 comma 8?	three fifths
~	Bob buys a 24-pack of pencils. Each pencil lasts for 3 days. If	57 [days]
4	he loses 5 of them, how many days will this pack of pencils	- • -
	last?	
F	A triangle has two sides of 5 and 6 centimeters. There are nine	54 [cm]
5	possible integer lengths for the third side. In centimeters,	- · [· · · ·]
	what is the sum of these nine possible lengths?	
	What is the number of cubic centimeters in the volume of a	36 pi [cm ³]
6	sphere with diameter 6 centimeters?	
		[
7	Solve the following equation for x: y squared minus x equals y	[x =] 3
	plus x, when y equals 3.	
8	How many prime numbers are between 30 and 84?	13 [prime
0		numbers]
0	What is the difference between the 3 rd largest and the 3 rd	499
9	smallest positive integer factors of 2012?	
10	Chuck has 3 dollars. If he has 3 times as many nickels as dimes	3 [dimes]
	and the same amount of guarters as nickels, how many dimes	
	does he have?	

7th & 8th Grade - December 1, 2012

COLLEGE KNOWLEDGE BOWL ROUND - EXTRA

#	Problem	Answer
1	How many unit cubes are needed to build four [PAUSE] three by three cubes?	108 [unit cubes]
2	What is the fourth smallest positive composite number?	9
3	In a book with 115 pages, how many times does the digit 6 appear among the page numbers, assuming every page is numbered.	21 [times]



		Final Score.
"Math is Cool"	Masters 2012-13	KEY
School:	Room # Team #	(Out of 8)
Name:	Proctor:	

7th & 8th Grade

Mental Math - 30 sec per question

Einal Coores

8 problems read orally to everyone - Approximately 8% of Individual Score - 25% of team score When it is time to begin, the proctor will read the first question twice. You may not do any writing or talking while arriving at a solution. Once you have a solution, record it on the sheet in front of you. You may not change or cross out answers once you have written an answer down. If there are eraser marks, writeovers, or crossed-out answers, they will be marked wrong. Once all students have laid their pencils on the desk, another question will be asked. If a student doesn't lay his/her pencil down, the maximum wait time is 30 seconds after completion of the second reading of the question before another question is asked. You may continue to work on a problem while the next questions. Individual scores used to determine individual placing will be determined by the sum of the Mental Math score and the Individual Test score for each individual. In addition, the top three Mental Math scores from one team will be totaled and doubled and will contribute to 25% of the team score.

	Answer	1 or 0	1 or 0
1	512 [bananas]		
2	10 [palindromes]		
3	30π [sq in]		
4	4		
5	South		
6	75 [percent]		
7	752		
8	3 [diagonals]		

Math is Cool" Masters – 2012–13 8th Grade – December 1, 2012 Student Name		score: EY
Student Name Proctor Name	Room # First	Score
SCHOOL NAME	Team # (out	of 20)

INDIVIDUAL MULTIPLE CHOICE - 15 minutes - 10 problems - 20% of team score

This test is the only test where you will be penalized for incorrect responses. You will receive 2 points for a correct letter response, 0 points for leaving it blank and -1 point for an incorrect response. It is not necessary to write your personal name on the test, but you may put it at the bottom of the test so your coach will be able to give you back the correct test. This test is taken individually, but it is part of your team score, including zeros for missing team members. Your team score will be calculated by taking the mean of your four team members' scores. When you are prompted to begin, tear off the colored sheet and begin testing. Since this is a multiple choice test, ONLY a letter response should be indicated as an answer on the answer sheet. No talking during the test.

	Answer	-1, 0 or 2	-1, 0 or 2				
1	В						
2	В						
3	D						
4	В						
5	E (58)						
6	D						
7	A						
8	D						
9	E (864 or 416)						
10	С						

*Math is Cool" Masters - 2 8th Grade - December 1, 20	Final Score:	
SCHOOL NAME	Team #	First Score
Proctor Name	Room #	(out of 10)

Team Contest - Score Sheet

TEAM TEST - 15 minutes - 30% of team score

When you are prompted to begin, tear off the colored sheet and give a copy of the test to each of your team members and begin testing. Each problem is scored as **1** or **0**. Record all answers on the colored answer sheet.

	Answer	1 or 0	1 or 0
1	5		
2	$\frac{175}{4}$		
3	4		
4	216 [cubic inches]		
5	1:15:20 AM		
6	176 [7 th graders]		
7	[n=] 2&7 [either order, both values required]		
8	261 [numbers]		
9	3√6 [<i>cm</i>]		
10	5/36		

"Math is Cool" Masters – 2012-13 8th Grade – December 1, 2012		Final Score:	
Proctor NameRoom #_		rst Score	
SCHOOL NAME	Team #_		

PRESSURE ROUND - 10 minutes - 5 problems - 5 rounds - 15% of team score

When it is time to begin, you will be handed a packet of five problems. There is a copy of the problems for each team member. Two minutes after the start of the test you are expected to submit an answer for one of the problems (it can simply be a guess). The maximum value of this answer is 1 point. In another two minutes you are expected to submit another answer to one of the four remaining problems; its maximum value is two points. This process will continue until all the problems are answered and each consecutive problem's worth will go up by one point. You must submit your answers on the colored sheets given to you. If you do not have an answer at the end of a two minute period, you must still submit an answer sheet with an identified problem number on it. Failure to do so will result in loss of points. This event is timed, and you will be given a verbal 5 second warning and told to hold your answer sheet up in the air. You may keep working as the sheets are collected. If a team answers the same question more than once, only the first answer will be scored and the other attempts will be ignored.

	Answer						
1	31/95						
2	20 [%]						
3	63 [cm ²]						
4	$\frac{172\pi}{3} + 32\sqrt{3} [cm^{2}] \text{ or } \frac{172\pi + 96\sqrt{3}}{3} [cm^{2}]$ or equivalent						
5	9 [days]						

Pressure Round Answers

		Fillal Scole.
"Math is Coo	l" Masters 2012-13	(Out of 8)
School:	Room # Team #	
Name:	Proctor:	
7 th & 8 th Grade	Mental Math - 30 sec per question	

Mental Math - 30 sec per question

Final Score:

8 problems read orally to everyone - Approximately 8% of Individual Score - 25% of team score When it is time to begin, the proctor will read the first question twice. You may not do any writing or talking while arriving at a solution. Once you have a solution, record it on the sheet in front of you. You may not change or cross out answers once you have written an answer down. If there are eraser marks, writeovers, or crossed-out answers, they will be marked wrong. Once all students have laid their pencils on the desk, another question will be asked. If a student doesn't lay his/her pencil down, the maximum wait time is 30 seconds after completion of the second reading of the question before another question is asked. You may continue to work on a problem while the next question is being read. The value of each question is a one or zero. Each student will be asked the same eight questions. Individual scores used to determine individual placing will be determined by the sum of the Mental Math score and the Individual Test score for each individual. In addition, the top three Mental Math scores from one team will be totaled and doubled and will contribute to 25% of the team score.

	Answer	1 or 0	1 or 0
1			
2			
3			
4			
5			
6			
7			
8			

N	Final Score:		
Student Name Proctor Name		Room #	First Score
SCHOOL NAM	NE	Team #	(out of 20)

INDIVIDUAL MULTIPLE CHOICE - 15 minutes - 10 problems - 20% of team score

This test is the only test where you will be penalized for incorrect responses. You will receive 2 points for a correct letter response, 0 points for leaving it blank and -1 point for an incorrect response. It is not necessary to write your personal name on the test, but you may put it at the bottom of the test so your coach will be able to give you back the correct test. This test is taken individually, but it is part of your team score, including zeros for missing team members. Your team score will be calculated by taking the mean of your four team members' scores. When you are prompted to begin, tear off the colored sheet and begin testing. Since this is a multiple choice test, ONLY a letter response should be indicated as an answer on the answer sheet. No talking during the test.

	Answer	-1, 0 or 2	
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			

"Math is Cool" Mas 8th Grade - Dece	Final Score:	
SCHOOL NAME	Team #	First Score
Proctor Name	Room #	(out of 10)

Team Contest - Score Sheet

TEAM TEST - 15 minutes - 30% of team score

When you are prompted to begin, tear off the colored sheet and give a copy of the test to each of your team members and begin testing. Each problem is scored as **1** or **0**. Record all answers on the colored answer sheet.

	Answer	1 or 0	1 or 0
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
	·		

December 1, 2012

STUDENT NAME: ______School Name: _____

Proctor Name: _____

Team #: _____Room #: _____

Final Score:

KEY

PRE-ALGEBRA Individual Contest - Score Sheet

	Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0
1	0			16	6 [cm]			31	28/1105		
2	8 [factors]			17	2.5 [ft/sec]	·		32	3 [ways]		·
3	165			18	75 [inches]			33	-[\$]45 or -[\$]45.00 or Lose [\$]45[.00]		
4	990			19	[x =] 1			34	44 [rectangles]		
5	11 [odd numbers]			20	80 [ft ²]			35	20 [cm ²]		
6	1/2			21	2			36	7.5 x 10 ¹⁶ [seconds]		
7	11 [regions]			22	146 [inches]			37	9/8		
8	9			23	6 [in.]			38	53		
9	5a - 3b + 3 [or Equiv]			24	2 [students]			39	(10, -3)		
10	3 [quadrants]			25	10 [units ²]			40	1465		
11	20 [gallons]			26	36 [mph]			3	1-40 TOTAL:		
12	1			27	18 [yds ³]						
13	1 [digi†]			28	8128			PRI	E-ALGEBRA		
14	[x=] 4			29	[x=] 11						
15	9 [sites]			30	[y=] 3						
1-	15 TOTAL:			16	-30 TOTAL:						

December 1, 2012

STUDENT NAME: ______School Name: _____

Proctor Name: _____ Team #: _____ Room #: _____

Final Score:

KEY

ALGEBRA Individual Contest - Score Sheet

	Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0
1	990			16	2 [students]			31	$\sqrt{6}[cm]$		
2	11 [odd numbers]			17	146 [inches]			32	-[\$]45 or -[\$]45.00 or Lose [\$]45[.00]		
3	165			18	[× =] 1			33	44 [rectangles]		
4	9			19	2			34	7.5 x 10 ¹⁶ [seconds]		
5	86 [integers]			20	[x=] 11			35	20 [cm ²]		
6	5a - 3b + 3 [or equiv]			21	$96+24\sqrt{2}$ [meters]			36	9/8		
7	1/2			22	6 [in.]			37	53		
8	3 [quadrants]			23	18 [yds ³]			38	(10, -3)		
9	[x=] 4			24	3√6			39	$y = -2x^2 + 4x + 30$		
10	8a + 12			25	4/9			40	1465		
11	20 [gallons]			26	36 [mph]			31-40 TOTAL:			
12	1			27	[y=] 3						
13	1 [digi†]			28	8128			ALGEBRA			
14	9 [sites]			29	28/1105						
15	6 [cm]			30	3 [ways]						
1-15 TOTAL:			16	-30 TOTAL:							

December 1, 2012

STUDENT NAME: ______School Name: _____

GEOMETRY Individual Contest - Score Sheet

	Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0		Answer	1 or 0	1 or 0	
1	86 [integers]			16	2 [students]			31	-[\$]45 or -[\$]45.00 or Lose [\$]45[.00]			
2	5a - 3b + 3 [or Equiv]			17	6 [in.]			32	44 [rectangles]			
3	$3\sqrt{2}$ [feet]			18	[x =] 1			33	7.5 x 10 ¹⁶ [seconds]			
4	1/2			19	2			34	20 [cm ²]			
5	672 [g]			20	8128			35	9/8			
6	3 [quadrants]			21	$96+24\sqrt{2}$ [meters]			36	53			
7	11 [regions]			22	6 [cm]			37	(10, -3)			
8	80 [ft ²]			23	18 [yds ³]			38	$12 - 8\sqrt{2}$ [in ²] or $4(\sqrt{2} - 1)^2$ [in ²] or equiv			
9	8a + 12			24	3√6			39	$y = -2x^2 + 4x + 30$			
10	6 [cm]			25	10 [units ²]			40	1465			
11	20 [gallons]			26	36 [mph]			3	1-40 TOTAL:			
12	[x=] 11			27	$4\sqrt{3}$ [m]							
13	1 [digi†]	·		28	28/1105			GEOMETRY				
14	146 [inches]			29	3 [ways]							
15	[y=] 3			30	$\sqrt{6} [cm]$							
1-15 TOTAL:			16	-30 TOTAL:								

