

“Math is Cool” Masters -- 2018-19


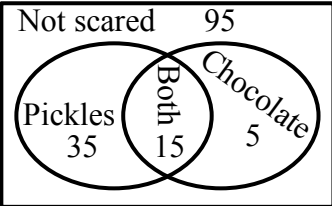
Middle School

Mental Math Solutions

7th	Answer	Solution
1	21 [miles]	$7 \times 3 = 21$
2	12 [days]	$.8 \times 15 = 12$
3	4 [inches]	$20/5 = 4$
4	3/4	{HH, HT, TH, TT} 3/4 of these have at least one H
5	14 [inches]	$r = \sqrt{194} = 14$
6	11	$(14 + 7 + 21 + 2)/4 = 11$
7	135 [degrees]	$6(180)/8 = 135$
8	10 [sets]	${}_5C_3 = 10$

“Math is Cool” Masters -- 2018-19
Middle School
Individual Test Solutions

7th	Answer	Solution
1	4408	$76 \times 58 = 4408$
2	885833	$8735207 - 7849374 = 885833$
3	2	$\sqrt{36} - \sqrt{16} = 6 - 4 = 2$
4	4.369×10^7	$a \times 10^b$ where a is a number between 1 and 10 and b is the number of places needed to move the decimal to the left to make a such a number
5	28 [inches]	$\sqrt{49} = 7 = \text{side length}, 4 \times 7 = 28 = \text{perimeter}$
6	1/663	Two red queens and two black jacks $2/52 \times 2/51 = 1/26 \times 2/51 = 1/13 \times 1/51 = 1/663$
7	$[x =] 3$	$7x/3 = 7 \rightarrow 7x = 21 \rightarrow x = 3$
8	9 [days]	If it doubles every day then it must have been half the size the day before. The day before day 10 is day 9.
9	6 [ways]	\$1 x 18 \$1 x 13 and \$5 x 1 \$1 x 8 and \$5 x 2 \$1 x 8 and \$10 x 1 \$1 x 3 and \$5 x 3 \$1 x 3 and \$5 x 1 and \$10 x 1,
10	9	$(3x + 2)(3x + 2) = 9x^2 + 12x + 4$ 9 is the coefficient of the x^2 term
11	105 [blips]	35 blips = 15 blaps, 15 blaps = 27 blops, so 35 blips = 27 blops, and 105 blips = 81 blops
12	2 or II	NE = Q1 and they are numbered in counterclockwise order. (-, +) is NW or Q2.

13	25	$ 3 - 4 \cdot 7 = 3 - 28 = -25 = 25$
14	20160 [ways]	$8!/2! = 40320/2 = 20160$
15	2 [zeros]	14! has a factor of 5 and a factor of 10. The factor of 10 means there will one zero at the end. The factor of 5 means there will be a 2 nd zero at the end since 5 times any even number ends in a zero.
16	53 [pencils]	$21 + 3 + 3 - 2 + 3 + 2 + 3 - 2 + 3 + 3 - 2 + 2 + 3 + 3 - 2 + 3 + 2 + 3 - 2 + 3 + 3 - 2 + 2 = 21 + 36 - 12 + 8 = 53$
17	295 ^[o]	The minute hand points to the 2 and the hour hand is 1/6 of the way between 4 and 5. $(1/6)30 = 5$. From 2 to 4 = 60 degrees. $60 + 5 = 65$. $360 - 65 = 295$ degrees.
18	ABDC	5683 +7462 13145, so A = 8, B = 4, C = 2, D = 3, so ABDC is greatest to least.
19	24	
20	95 [people]	 <p>All four numbers add up to 150, the numbers in the Pickles circle add up to 50, and the numbers in the Chocolate circle add up to 20. So the answer is 95.</p>
21	40 [minutes]	Focus on Eho. Ten minutes to go, come back and get backpack. Then thirty more to walk a mile, for a total of 40.
22	\$3121.20 or 3121 dollars and 20 cents	$3000(1.02) = 3060$ $3060(1.02) = 3121.20$
23	44 [cubes]	Only cubes on the edges and the corners will have two or three faces painted. The rest have only one face or zero faces painted. There are 8 vertices and 12 edges. Subtract 2 (for the corners) from 5 to get the number of cubes on the edges. So the answer will be $12 \times 3 + 8 = 44$.

24	1 [hole]	3 holes with 1 putt and 2 putts on the other 15 holes makes a total of 33 putts. $47 - 33 = 14$ If he has one extra putt on 14 of the 15 holes with at least 2 putts, he could conceivably have just one hole with 2 putts.
25	22/105	$P(gg) = 3/15 \times 2/14 = 6/210$ $P(bb) = 4/15 \times 3/14 = 12/210$ $P(br,br) = 3/15 \times 2/14 = 6/210$ $P(bl,bl) = 5/15 \times 4/14 = 20/210$ $(6+12+6+20)/210 = 22/105$
26	13/16	$P(\text{at least 2 H}) = 1 - P(0H \text{ or } 1H)$ $1 - (1/32 + 5/32) = 26/32 = 13/16$
27	11 [cows]	Let a = chickens, b = cows $(3a + 5b = 73)(2) \rightarrow 6a + 10b = 146$ $(2a + 3b = 45)(-3) \rightarrow -6a - 9b = -135$ Add the two new equations: $b = 11$ cows
28	$5\sqrt{5}$ [inches]	$3^2 + 6^2 = c^2 \rightarrow 9 + 36 = c^2 \rightarrow 45 = c^2 \rightarrow c = 3\sqrt{5} = \text{hypotenuse}$ of the triangle with legs 3 and 6. Then because the triangles are similar: $6/(6 + 4) = 3\sqrt{5}/x \rightarrow 6x = 30\sqrt{5} \rightarrow x = 5\sqrt{5}$
29	5	$x^2 - 5x - 50 = 0$ $(x - 10)(x + 5) = 0$ $x = 10$ and $x = -5$, and $10 + -5 = 5$
30	$54\sqrt{3}$ [in ²]	A regular hexagon is made of 6 equilateral triangles. For an equilateral triangle, the formula is $A = s^2\sqrt{3}/4$, so for a hexagon it will be $6(6^2\sqrt{3}/4) = (216/4)\sqrt{3} = 54\sqrt{3}$
31	66 [seconds]	$r_1 = d/t$ and $r_2 = d/60$, $r_2 = 1.1r_1 = 1.1d/t \rightarrow d/60 = 1.1d/t \rightarrow 1/60 = 1.1/t \rightarrow t = 66$ seconds
32	13.5	$S = a_1/(1-r)$ or $S = 9 + 3 + 1 + \dots$ $(1/3)S = 3 + 1 + \dots$ Subtract equations $(2/3)S = 9 \rightarrow S = 9(3/2) = 13.5$

33	1/26	<p>1,3,9,347 2,6,18,334 3,9,27,321 ... 9,27,81,243 – ratio of 1:3:9:27 ... 26,78,234,22 27,81,243,9</p> <p>If you write the list of strings of numbers where the first three are in a ratio of 1:3:9, it looks like the list above. At first, it seems like there are 27 possibilities, but it turns out that the last one in the list has the same four numbers as the one with 9,27,81,243.</p>
34	14 [ordered pairs]	$9\pi a + 9\pi b/3 = 132\pi$ simplifies to $3a + b = 44$ Starting with $a = 1$, there are 14 integer solutions to this equation
35	[q =] 4800	Even multiples of 13 include 26, 52, 78, 104, etc. Even multiples of 17 include 34, 68, 102, etc. The only pair from these two lists that are close enough together to be part of a set of three consecutive even integers are 102 and 104. Then the smallest possible third of the three consecutive even integers would be 100. The prime factorization of $100 \times 102 \times 104$ is $2 \times 2 \times 5 \times 5 \times 2 \times 3 \times 17 \times 2 \times 2 \times 2 \times 13$. If you multiply this out without the 13 or 17 included, you get 4800.
36	702	$(x + 1/x)^2 = x^2 + 2 + 1/x^2 = 81$ So $x^2 + 1/x^2 = 79$ $(x + 1/x)(x^2 + 1/x^2) = 9 \times 79 = 711$ $x^3 + 1/x + x + 1/x^3 = 711$ $x^3 + 1/x^3 + x + 1/x = 711$ $x^3 + 1/x^3 + 9 = 711$ $x^3 + 1/x^3 = 702$ or use the pattern $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$ to expand $(x + 1/x)^3 = 729$ and solve that way.
37	3/6622	44 cards total, three 6s, two 12s, one 18 $(3C1 \times 2C1 \times 1C1)/44C3$ or $1/44 \times 2/43 \times 3/42 \times 6$

38	[C =] 46	When $S = 6$, there are three terms, $15x^4y^2$, $16x^3y^3$, and $15x^2y^4$. $15 + 16 + 15 = 46$
39	17/988	The number of sets of 3 distinct 2-digit integers is ${}_{40}C_3 = (40 \times 39 \times 38) / (3 \times 2 \times 1) = 9880$. Sets where the median = the mean are as follows: $\{10, 11, 12\}, \{11, 12, 13\}, \dots, \{47, 48, 49\} \rightarrow 38$ $\{10, 12, 14\}, \dots, \{45, 47, 49\} \rightarrow 36$ $\{10, 13, 16\}, \dots, \{43, 46, 49\} \rightarrow 34$ $\{10, 14, 18\}, \dots, \{41, 45, 49\} \rightarrow 32$ $\{10, 15, 20\}, \dots, \{39, 44, 49\} \rightarrow 30$ $(30 + 32 + 34 + 36 + 38) / {}_{40}C_3 = 170 / 9880 = 17 / 988$
40	[n =] 10	b must be 4, 5, 6, 7, 8, or 9 Check them all $123_4 = 27$, $123_5 = 38$, $123_6 = 51$, $123_7 = 66$, $123_8 = 83$, and $123_9 = 102$, so all of them meet the first condition. Then check $321_4 = 57$, $321_5 = 86$, $321_6 = 121$, $321_7 = 162$, $321_8 = 209$, and $321_9 = 262$. It only meets the second condition when $b = 9$ and $(10 + 6)^2 + 6 = 262$. So, $n = 10$.
41	13	$-9x + 9y + 8z = 155$ and $-9(-x - 2y + 5z = 83)$ added together is $27y - 37z = -592$ $2(-x - 2y + 5z = 83)$ and $2x - 5y + 5z = 74$ added together is $-9y + 15z = 240$ $-3(9y + 15z = 240)$ and $27y - 37z = -592$ added together is $8z = 128$, so $z = 16$ $9y + 15(16) = 240$ means that $y = 0$ $-x - 2(0) + 5(16) = 83$ means that $x = -3$ $-3 + 0 + 16 = 13$
42	[d =] 117	From the first equation you can see that $b \times c$ must equal 8 and by solving the second equation you get that $b + c = a$. So, when $b = 1$ and $c = 8$, then $a = 9$. When $b = 2$ and $c = 4$, then $a = 6$. Swapping the values of b and c in each of these cases gives the same value of a . Since $a^2 = d$, there are two possible values of d , 6^2 and 9^2 and $36 + 81 = 117$.

43	36/7 [ft]	<p>Let $y = x$ and the right and left segments that add up to 6 be y and $6 - y$ Then $x/12 = y/6$ and $x/9 = (6 - y)/6$ So $6x = 12y$ and $6x = 54 - 9y$ $12y = 54 - 9y$ $y = 18/7$ $x/12 = 18/42$ $x = 216/42 = 36/7$</p>
44	13 [cm]	<p>Solve for the radius of the sphere $(4/3)\pi r^3 = 2304\pi$ $r = 12$ If x is the side length of the cube, then $x\sqrt{3} = 24$ and $x = 8\sqrt{3}$ $8 \times 1.7 = 13.6$ So, the largest integer less than 13.6 is 13</p>
45	$\sqrt{3}/3$ or $\frac{1}{\sqrt{3}}$	<p>Points chosen on the circle result in right triangle, points outside the circle result in acute triangles, points inside the circle result in obtuse triangles. The height of the triangle is 1 so half of a side is $1/\sqrt{3}$, meaning the perimeter is $2/\sqrt{3}$. The parts of \overline{AO} and \overline{BO} that are inside the semicircle are each of length 1. To get the answer simplify $2/(2/\sqrt{3})$. Points O, C, and the other two intersections of the triangle and the semicircle are dimensionless, so they do not effect the probability</p>

“Math is Cool” Masters -- 2018-19

Middle School

Multiple Choice Solutions

7th	Answer	Solution
1	E	A(-6, 8) and A'(-6, -8) From 8 to -8 is 16 units
2	D	C(-4, 4), C'(4, 4), C''(4, -11) $CC'' = \sqrt{(-4 - 4)^2 + (4 - -11)^2} = \sqrt{64 + 225} = \sqrt{289} = 17$
3	D	A(-6, 8) $\Rightarrow (-6)^2 + 8^2 = 100$, OA = 10, area = 100π B(-9, 6) $\Rightarrow (-9)^2 + 6^2 = 117$, OB = $\sqrt{117}$, area = 117π C(-4, 4) $\Rightarrow (-4)^2 + 4^2 = 32$, OC = $\sqrt{32}$, area = 32π D(-5, 7) $\Rightarrow (-5)^2 + 7^2 = 74$, OC = $\sqrt{74}$, area = 74π Area ratio is $32\pi : 74\pi : 100\pi : 117\pi$, which simplifies to 32:74:100:117
4	C	6,929,725,043 in scientific notation is 6.929725043×10^9 and if the decimal number is rounded to the nearest hundredth, it would be 6.93×10^9
5	E	3.4 hundred million - 0.5 hundred million = 2.9 hundred million $2.9/0.5 = x/100$ $x = 290/0.5 = 580$

6	B	<p>2.5% of 4 billion is 100 million</p> $\begin{array}{r} 4,000,000,000 \\ - \underline{100,000,000} \\ 3,900,000,000 \end{array}$ <p>2.5% of 3,900,000,000 is 97,500,000</p> $\begin{array}{r} 3,900,000,000 \\ - \underline{97,500,000} \\ 3,802,500,000 \end{array}$ <p>2.5% of 3,802,500,000 is 95,062,500</p> $\begin{array}{r} 3,802,500,000 \\ - \underline{95,062,500} \\ 3,707,437,500 \end{array}$ <p>3,707,437,500 – this is the answer</p>
7	B	<p>(0, 0), (1, 1), (2, 2), (3, 3), (4, 4), (5, 5), and (6, 6) are all of the doubles. There are 7 out of 28 total tiles. $7/28 = 1/4$</p>
8	C	<p>There are a total of 8 of each number from 0 to 6, so $8(0 + 1 + 2 + 3 + 4 + 5 + 6) = 8(21) = 168$</p>
9	E	<p>To calculate the number of tiles in a double-twelve set: there are 13 tiles in the list (0, 0), (0, 1), (0, 2), ..., (0, 12), 12 tiles in the list (1, 1), (1, 2), (1, 3), ..., (1, 12), 11 tiles in the list (2, 2), (2, 3), (2, 4), ..., (2, 12), and so on until the last list is the one tile (12, 12). So the total is $1 + 2 + 3 + \dots + 11 + 12 + 13 = 91$</p>
10	A	<p>Double-six set has 28 total tiles $(1+2+3+4+5+6+7)$ Double-nine set has 55 total tiles $(1+2+3+4+5+6+7+8+9+10)$ $P((6, 4), \text{ then } (3, 5)) \text{ in double-six set} = 1/28 \times 1/27$ $A = 1/(28 \times 27)$ $P((6, 4), \text{ then } (3, 5)) \text{ in double-nine set} = 1/55 \times 1/54$ $B = 1/(55 \times 54)$ $28 \times 27 = 2 \times 2 \times 7 \times 3 \times 3 \times 3$ $55 \times 54 = 5 \times 11 \times 2 \times 3 \times 3 \times 3$ LCM of $(2 \times 2 \times 7 \times 3 \times 3 \times 3)$ and $(5 \times 11 \times 2 \times 3 \times 3 \times 3)$ is $2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 7 \times 11$</p>

“Math is Cool” Masters -- 2018-19
Middle School
Team Test Solutions

7th	Answer	Solution
1	5.5 [hours]	$165/55 + 175/70 = 5.5$
2	11 [prime numbers]	23,29,31,37,41,43,47,53,59,61,67
3	34	$34 + 35 + 36 + 37 = 142$ $3+4+3+5+3+6+3+7=34$
4	38 [Ruby-Throated Hummingbirds]	5/12 of 228 is 95 Ruby-Throated Hummingbirds, so there are 133 Bee Hummingbirds. $133 - 95 = 38$
5	441	$21^2 = \text{sum of } 1^{\text{st}} \text{ } 21 \text{ odd integers} = 441, \text{ or just add them.}$
6	5 [shots]	Make 4, miss, make 4, miss, make 4, miss, make 5 All other scenarios involve longer streaks
7	$5\sqrt{2}$ [inches]	$d = \sqrt{3^2 + 4^2 + 5^2} = \sqrt{50} = 5\sqrt{2}$
8	-1	The coordinates are: $A(-3, 4)$ and $A'(4, -3)$ Slope of $\overline{AA'}$ = $(4 - -3)/(-3 - 4) = -1$
9	4/5	There are 5 multiples of 8 between 0 and 41, between 41 and 82, between 82 and 123, etc. Only the last of these 5 multiples will be followed either by a hippo yawn or a simultaneous tick consumption and hippo yawn. Therefore, 4 out 5 times is the answer.

<p>10</p>	<p>72 [paths]</p>	<p>ABCDE, ABEDC, ACBDE, ACBED, ACDBE, ACDEB, ADCBE, ADEBC, AEBCD, AEBDC, AEDBC, AEDCB – 12 that start with A There are also 12 that start with B CABDE, CABED, CADBE, CADEB, CAEBD, CAEDB, CBADE, CBAED, CBDAE, CBDEA, CBEAD, CBEDA, CDABE, CDAEB, CDBAE, CDBEA, CDEAB, CDEBA – 18 that start with C There are also 18 that start E DACBE, DAEBE, DBCAE, DBEAC, DCABE, DCAEB, DCBAE, DCBEA, DEABC, DEACB, DEBAC, DEBCA – 12 that start with D</p>

“Math is Cool” Masters -- 2018-19
 Middle School
Relay Solutions

7th	Answer	Solution
1-1	46 [centimeters]	$2(15 + 8) = 46$
1-2	45	1,2,23.46 $46 - 1 = 45$
1-3	[x =] 21	$3.5/7.5 = x/45$ $x = 21$
1-4	3 [values]	$1+2+3+4=5+6 \rightarrow X = 6$ $6+7+8 \rightarrow X = 3$ $10+11 \rightarrow X = 2$ 3 values
2-1	12	$42 = 2 \times 3 \times 7$ $2+3+7 = 12$
2-2	1728	$12^3 = 1728$
2-3	95 [multiples]	$96 \times 18 = 1728$, so 95 multiples are less than 1728
2-4	19	$95 = \sqrt{475D}$ $95 \cdot 95 = 475D$ $D = \frac{95 \cdot 95}{25 \cdot 19} = 19$

“Math is Cool” Masters -- 2018-19
Middle School

College Bowl Round #2 Solutions

7th	Answer	Solution
1	3/10 or “3 over 10” or “3 out of 10”	$P(3 \text{ blue in a bag with } 10 \text{ total}) = 3/10$
2	East	$90 \times 7 = 630 = 360 + 270$ Starting from north, 270 CCW = East
3	6 [candies]	Start with 21, Jean gets 9, 12 left, I eat 6, 6 left.
4	20 [diagonals]	$n(n-3)/2$ $8(5)/2 = 20$
5	6.4 [hours]	$8Z = 8H$, $2Z = 32H$ (or 4 times as long as 8Z), $10Z = (32/5)H$ (or 1/5 as long as 2Z) = 6.4H
6	[x=] 16	$x + y = 50$, $2x + 2 = y$, $x + 2x + 2 = 50$, $3x = 48$, $x = 16$
7	5:20 am	$60 \times 33 = 1980 \rightarrow 2000 \text{ min} = 33 \text{ hrs}, 20 \text{ min} \rightarrow 33 \text{ hrs}, 20 \text{ min} - 24 \text{ hrs} = 9 \text{ hrs}, 20 \text{ min} \rightarrow 8 \text{ PM} + 9 \text{ hrs}, 20 \text{ min} = 5:20 \text{ am}$
8	4/11 or “4 over 11” or “4 to 11”	10-39 is 30 numbers 8 primes: 11, 13, 17, 19, 23, 29, 31, 37 The rest (= 22) are composite $8/22 = 4/11$
9	4.3 [miles]	6 mi in 60 min \rightarrow .1 mi in 1 min \rightarrow 4.3 mi in 43 min
10	288π [in ³]	$V = 4/3\pi r^3$ $4/3\pi(6^3) = 4/3\pi(216) = 4\pi(72) = 288\pi$

“Math is Cool” Masters -- 2018-19
Middle School

College Bowl Round #3 Solutions

7th	Answer	Solution
1	4.2 [times]	$21/5 = 4.2$
2	95	$97 - 2 = 95$
3	104 [degrees]	Sum of angles of a quadrilateral = 360 $360 - 60 = 300$ $(300)/3 = 100$
4	36 [cm ³]	Smallest possible values of A, B and C are A = 3, B = 2, C = 6 $V = 3 \times 2 \times 6 = 36$
5	14	$ab = 147, a = 3b \rightarrow 3b^2 = 147 \rightarrow b^2 = 49 \rightarrow b = 7$ and $a = 21$ $21 - 7 = 14$
6	200 [skittles]	A minimum of 100 each of 4 colors = 400 The rest could be the fifth color = 200
7	19/26 or “19 out of 26” or “19 over 26”	6 red face cards, 4 aces, 4 twos = 14 winning cards and 38 losing cards $38/52 = 19/26$
8	330	$LCM(60, 150) = 300$ $GCF(60, 150) = 30$ $300 + 30 = 330$
9	[0].45	$11/5 - 7/4 = (44 - 35)/20 = 9/20 = 0.45$
10	6 [ways]	$4!/(2!2!) = 6$

“Math is Cool” Masters -- 2018-19
Middle School

College Bowl Round #4 Solutions

7th	Answer	Solution
1	10	$6 \times 99 = 594$, the closest multiple of 11 less than 604 $604 - 594 = 10$
2	228	$19(3 + 21)/2 = 228$
3	38 [free throws]	$(7 + x)/(12 + x) = 9/10$ $70 + 10x = 108 + 9x$ $x = 38$
4	115 [%]	$p/100(7000)=8050$ $p=8050(100)/7000 = 115$
5	7	Ignore the two thousand part $15^3 = 3375$, so 7
6	20 [factors]	$648 = 2^3 \times 3^4$ Total number of factors = $(3 + 1)(4 + 1) = 20$
7	64π [ft ²]	$d = 8$, $r = 4$, $SA = 4\pi r^2$ $4\pi(4)^2 = 64\pi$
8	7 [integers]	105, 120, 135, 150, 165, 180, 195 – 7 integers
9	119	$7/12 + 2/5 = (35 + 24)/60 = 59/60$ $59 + 60 = 119$
10	20 [palindromes]	22, 33, 44, 55, 66, 77, 88, 99, 101, 111, 121 131, 141, 151, 161, 171, 181, 191, 202, 212 – 20 palindromes

“Math is Cool” Masters -- 2018-19

Middle School

College Bowl Round #5 Solutions

7th	Answer	Solution
1	6 [years old]	$\frac{1}{4}$ of 24 = 6 He'll be 30 in 24 years, which is 5 times 6.
2	11/15 [beats per second] or “11 over 15”	44 beats in 60 sec = $\frac{44}{60}$ beats per sec = 11/15
3	[x =] 8	$x + 19 = \frac{3}{5}(45)$ $x + 19 = 27$ $x = 8$
4	\$38.04 or 38 dollars and 4 cents or thirty-eight-oh-four	$4 \times 2.99 = 11.96$ $50 - 11.96 = 38.04$
5	28 [centimeters]	Shortest possible: $A > 19 - 15 > 4$ or 5 Longest possible: $A < 19 + 15 < 3$ or 33 $33 - 5 = 28$
6	11/40 or “11 out of 40” or “11 over 40”	$3 \times 13 = 39$, so 13 multiples of 3. Multiples of 3 that are also multiples of 5 are multiples of 15. There are 2 multiples of 15 less than 40. $13 - 2 = 11 \rightarrow 11/40$
7	14 [prime factors]	Just count the prime numbers less than 46: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43 \rightarrow 14 prime factors
8	16 [oranges]	$6B = 10A$ and $5A = 12O \rightarrow 10A = 24O \rightarrow 6B = 24O \rightarrow 4B = 16O$
9	124	$3^2 - 4 = 5$, $5^3 - 5^2 + 7(5) - 11 = 124$
10	36 [cows]	$c/s = \frac{2}{5}$, $c/\text{total} = \frac{2}{7}$, $\frac{126}{7} = 18$, $2 \times 18 = 36$ cows

“Math is Cool” Masters -- 2018-19
Middle School

College Bowl Round #6 Solutions

7th	Answer	Solution
1	[x =] 7	$400x - 600 = 2200$ $400x = 2800$ $x = 7$
2	16/81	$(2/3)^4 = 16/81$
3	6 [multiples]	27, 36, 45, 54, 63, 72 = 6 multiples
4	5.6	$(2 + 3 + 5 + 7 + 11)/5 = 5.6$
5	9 [cards]	If Eman only had the Edwin Diaz card, then Connor must have traded 12 cards to her for it. If Eman had more than just the Edwin Diaz card, then Connor would have traded fewer cards for it, so that Eman ended up with 12 cards. Therefore, the scenario in which Connor traded 12 cards is the one in which he has the greatest number of cards to start with. In order for Connor to have 12 cards after trading with Bella, he must have had 9 to start with ($9 + 4 - 1 = 12$).
6	594	$A/B = C/D$ and $B = 6A \rightarrow A/6A = 1/6 = C/D$ C is a 2-digit number. To maximize the value of D, C must be 99 $\rightarrow 99/D = 1/6 \rightarrow 6(99) = D = 594$
7	784π [cm ³]	$14^2\pi(4) = 784\pi$
8	4 [minutes]	$.9(150) = 135$ $540/135 = 4$ min
9	Sunday	$7 \times 17 = 119$ $120 - 119 = 1$ 1 day after Saturday is Sunday
10	12 [centimeters]	$A = bh/2$ and $b = 2h \rightarrow 2h(h)/2 = 36 \rightarrow h^2 = 36 \rightarrow h = 6 \rightarrow b = 12$

“Math is Cool” Masters -- 2018-19
Middle School
College Bowl Round (Extra) Solutions

7th	Answer	Solution
1	[x =] 24	$6x - 11 = 4x + 37$ $2x = 48$ $x = 24$
2	56 [centimeters]	$\sqrt{196} = 14$ $14 \times 4 = 56$
3	24 [ordered pairs]	(26, 24), (27, 23), . . . , (48, 2), (49, 1) $49 - 25 = 24$ pairs
4	11/12	$(6 - -5)/(3 - -9) = 11/12$
5	39601	$(200 - 1)(200 - 1) = 40000 - 2(200)(1) + 1 = 40000 - 400 + 1 = 39601$
6	11/45	12 to 96 = 4(3) to 4(24), so 22 multiples of 4 out of 90, $22/90 = 11/45$
7		
8		
9		
10		