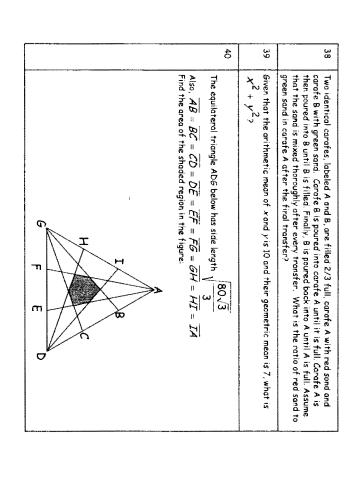
Sponsored by: Kimberly- Clark 9th and 10th Grade - May 10, 2003 Individual Contest

Express all answers as reduced fractions unless stated otherwise. Leave answers in terms of π where applicable. Do not round any answers unless stated otherwise. Record all answers on the colored cover sheet.

13	12	11	10	9	0.0	7	6	UTI	4	W	2		
Simplify $5\sqrt{75}+8\sqrt{27}-11\sqrt{48}$ to the form $a\sqrt{b}$ where b does not have a factor that is a perfect square. Find a + b.	A rectangle has diagonals of length 10. The area of the rectangle is 48. The side lengths are integral values. What is the perimeter of the rectangle?	What is the hundreds digit of 5 ²⁰⁰³ ?	Solve for all real values of x: $7(x-5)^3 + 12 = 68$	A wheel on a car with radius 22/π inches is rotating at 120 revolutions per minute. How fast is the car traveling in miles per hour?	While hiking Sarah and Dillon notice that they can gain 30 feet of elevation every minute at 4000 feet and 16 feet per minute at 7000 feet. Suppose that this data is used to determine a linear model predicting their rate of elevation gain as a function of altitude. According to this model, how many feet per minute would they be able to gain at 10,000 feet?	What is the maximum number of times a circle and parabola can intersect?	Jamie ran 3.5 miles in 19 minutes and 15 seconds. If she ran at a constant rate the entire race, how many seconds did it take her to run one mile?	What is the slope of the line perpendicular to $7x - 3y = 10$?	What is the sum of the x-coordinates of the x-intercepts of $f(x) = -3x^2 + 5x + 72$	Is the following system of linear equations consistent or inconsistent? 2y = 14 -8x 16x + 4y - 28 = 0	The midpoint of the line segment whose endpoints are (3,-2) and (15,18) is (a, b). Find a + b.	Solve for all values of x : $5(3x+2) = 7(2x+9)$	

4	Find the measure of angle B in degrees, in the circle shown, if the length of the line segment AB is 1, O is the center of the circle, and the length of the line segments AO and BO is $\frac{\sqrt{2}}{2}$.
55	Find the vertex of the parabola described by: $y = x^2 + 4x + 3.$
16	What is the equation, in slope-intercept form, for a line with an x-intercept of (6,0) and a y-intercept of (0,4)?
17	In a 5-6-8 triangle, what is the ratio of the langest altitude to the shortest altitude?
18	Two points (a,b) and (c,d) on the curve defined by $f(x)=x^2$ are five units away from $(6,1)$. Find the sum of a,b,c & d .
19	What is the area of the ellipse defined by $\frac{(x+3)^2}{16} + \frac{(y-4)^2}{25} = 12$
20	5 coms were flipped at once. There were exactly x heads showing. The probability that this event would occur is 5/16. What is the sum of all possible values of x^2
21	Solve for x: $\frac{5^{x^2}}{5^5x} = \frac{1}{625}$.
22	In triangle \overline{ABC} , \overline{AB} = 5, \overline{BC} = 6 and \overline{AC} = 7. Let \overline{D} be on \overline{BC} such that \overline{AD} is the bisector of \overline{AC} . What is the length of \overline{DC} ?
23	What is the smallest positive integer greater than 1 that is a perfect square, cube and fourth pawer?
24	Take a 3-digit number. Subtract from it the same number with the digits reversed (ex. 543-345). If the result of such an operation is 99, what is the largest possible original number?
25	Solve for all real values of x: $\sqrt{x+10} - \frac{6}{\sqrt{x+10}} = 5$
26	Given a 10th degree polynomial with 10 negative coefficients and 1 positive coefficient, what is the maximum number of positive roots it can have?
27	Consider $f(x) = 2x^2 - 4x + c$. What value of c maximizes the product of the roots of $f(x)$, given that at least one root is real?

37	35	34	33	32	31	30		29	28
What is the product of the four complex fourth roots of 812 Evaluate the sum 1 1 1 1 1 1 1 $3+\sqrt{7}+\sqrt{5}+\sqrt{5}+\sqrt{5}+\sqrt{3}+1$	Triangle ABC is inscribed inside circle O. If $\angle A=60^\circ$, $\angle B=45^\circ$, $\angle C=75^\circ$ and the radius of circle O is 1. What is the area of $_0ABC$?	How many positive integer factors does 3^{12} - 2^{12} have?	A circle with radius 6 is surrounded by 3 larger congruent circles, so that every circle touches oll 3 other circles. What is the radius of the larger circles?	Consider points A, B, C, and D in that order on a line (, where AC:BD = 3:7, and BC:AD = 1:4. Determine AB:CD.	A point is chosen at random from the interior of triangle ABC. What is the probability that it is closer to vertex C than vertices A and B? 3 5 8 4 C	Simplify: 484848	Challenge Questions	The number 151 in base 10 is written in base 12. How many zeros does it end with?	What is the sum of the squares of the roots of $4x^2 + 3x + 2 = 0$?



MATN IS COO!" CHAMPIONShips-2003 Sponsored by: Kimberly-Clark and Lukins & Annis PS 9th, 10th, 11th & 12th Grade - May 10, 2003 Individual Multiple Choice Contest

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•	00	7	6	O1	4	ω	2	-
What is the first time after 3:00 when the hour and minute hands of a 12-hour analog clock are 120° apart? A)3:38:10 B) $3:38:10\frac{10}{11}$ C) $3:38:10\frac{14}{15}$ D) $3:38:11$ E) Answer not given	What is the largest number of points in which three triangles (which do not share any portions of sides) can intersect? A) 12 B) 13 C) 14 D) 15 E) Answer not given	Solve for x in the following equation for x in terms of a, b, c and d: $a - cx + bx^2 = d$ A) $\frac{c \pm \sqrt{c^2 - 4b}}{2b} \text{B} \frac{c \pm \sqrt{c^2 - 4b(a - d)}}{2b} c \frac{c \pm \sqrt{4b(a - d)}}{2b}$ D) $\frac{c \pm \sqrt{c^2 - 4b(a - d)}}{2} \text{E) Answer not given}$	What is the equation of the directrix of the parabola $x^2 + 8y = 0$? A) $y = 2 B$ $y = -2 C$ $x = 2 D$ $x = -2 E$ Answer not given	What shape is the graph of $4x^2 - 3x + 2y^2 - 8 = 0$? A) straight line B) parabola C) hyperbola D) ellipse E) Answer not given	Factor completely: $4a^2 - 9b^2 - c^2 - 6bc$ A)(2a-3b-c)(2a+3b-c) B) (2a-3b-c)(2a-3b+c) C) (2a-3b-c) ² D) (2a+3b+c) ² E) Answer not given	How many natural numbers are 4 digits long when expressed in base 8, but 5 digits when expressed in base 6? A) 2800 B) 421 C) 2600 D) 821 E) Answer not given	What is the equation of a parabola passing through the points (1, 2), (-3, 14) and (3, 20). A) $\gamma = 5x + 3$ B) $\gamma = 2x^2 + x - 1$ C) $\gamma = -x^2 + 7x - 4$ D) $\gamma = x^2 + 3x - 2$ E) Answer not given	What is the remainder when $6x^3 + 10x^2 + x + 8$ is divided by $2x^2 + 12$ A) $-2x + 3$ B) 0 C) $-3x + 5$ D) $4x + 6$ E) Answer not given

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Leave answers in terms of π where applicable.

Do not round any answers unless stated otherwise.

Recard all answers on the colored cover sheet

Reco	Record all answers on the colored cover sheet.
-	Consider the 4x4x4 array of lattice points whose coordinates are either 0, 1, 2, or 3. How many right rectangular solids have eight of these points as vertices and have edges of integer length?
2	Three real numbers are randomly chosen between 0 and 10. What is the probability that their sum is less than 10?
ω	Consider a process in which a three-digit number (e.g. 246) is concatenated with itself reversed (e.g. 642) to produce a 6-digit number (e.g. 246642). What is the largest natural number which is guaranteed to be a factor of possible 6-digit numbers produced by this process?
4	Express $0.08\overline{3}_9$ as a fraction (base 10) in lowest terms.
(Ji	What is the tens digit of $6^{315} + 3^{11}$?
6	What is the largest integer by which all even, perfect squares must be divisible?
7	What is the length of the semi-major axis of the ellipse defined by the equation $4x^2 + y^2 + 32x - 4y + 52 = 0$?
8	If c chickens can lay e eggs in d days; how many days will it take r fewer chickens to lay the same number?
9	What is the determinant of $\begin{bmatrix} 1 & 3 \\ -2 & 1 \end{bmatrix}$?
10	Eho is shooting free throws. He makes his first shot and misses his second shot. For each shot after the second, the probability that he makes that particular shot is equal to the ratio of the number of successful shots to the number of attempted shots. What is the probability that Eho will have made exactly 50 shots after 100 attempts?

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"Math is Cool" Masters-2003

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Express all answers in terms of radicals and π_{c} where applicable, unless otherwise instructed.

Pers	Person #1	
	How many prime numbers less than 30 are divisible by 32	1
N	Evaluate: $\sqrt{8^2+15^2}$ Read as: Evaluate the square root of the quantity eight squared plus fifteen squared	17
ω	What is the geometric mean of 12 and 108?	36
4	Solve for $x: 2^r = 1024$ Read as: solve for $x:$ two to the power x equals 1024.	[x =] 10
Pers	Person #2	
-	What is the measure, in degrees, of one interior angle of a regular pentagon?	108["]
2	What is the sum of the reciprocals of the first three primes?	31/30
ω	What is the surface area of a sphere with radius 🛂	π
4	Solve for $x: 2x^2 - 3x + 1 = 0$. Read as: Solve far x : two times x squared minus 3 times x plus 1 equals xero.	x=1 or x=1/2 Both answers needed
Pers	Person #3	
-	What is the slope of a line with x-intercept (12, 0) and y-intercept (0, 8)?	-2/3
2	What is the greatest cammon factor of 196 and 280?	28
w	What is the maximum possible volume of a rectangular prism with a surface area of 24 square centimeters?	8 [cm³]
4	If the sum of three consecutive integers is 1560, what is the largest number?	521
Pers	Person #4	
	How many diagonals can be drawn in a regular octagon?	20
2	If $a \cdot b = 90$, and a and b are both primes, what is the largest possible value of a^2	83
Ĺ,	Write as a repeating decimal: 6/11	.545454 or
4	A cylinder filled with maple syrup has a radius of 2 and a height of 27. If it is emptied into 3 congruent spheres, and each are completely filled, what is the radii of the spheres?	Ĺ

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8			7	6	Ŋ	4	ω	73	-	
An urn contains 8 orange marbles and 12 black marbles. If two marbles are drawn without replacement, what is the probability they are the same color?	Number $ ot\! g$ is an extra question. Only use it if needed.	Read as: For what values of x is the following inequality true? The quantity $x + 3$ divided by the quantity $x + 3$ is less than or equal to 0.	For what values of x is the following inequality true? $\frac{x+3}{x+3} \le 0$	7, a, b, c, 11 is an arithmetic sequence. What is b?	At what point does the line $3x + 5y = 8$ intersect the line $-2x + 7y = 5$?	What are the coordinates of the point on the segment AB that is two-thirds of the way from A to B, where A has coordinates (2,4) and B has coordinates (-1,1)?	How many points with integer coordinates are exactly 6 units away from (0,0)?	How many natural numbers less than 1000 are multiples of both 6 and 8?	If Jason flipped 6 fair coins, what is the probability of his getting at least 2 heads?	College Knowledge Bowl Questions #1
47/95		no value exists or null set	None or empty set	9	(1,1)	(0,2)	4	41	57/64	

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œ		7	6	Çī	4	ω	7	H	
Eric has a die weighted so that it is twice as likely to roll an even number as it is to roll an odd number. Suppose he rolls the die twice. What is the probability that the numbers he gets sum to 7?	Number $oldsymbol{g}$ is an extra question. Only use it if needed.	Find the y-intercepts: x^2 -8x +y ² + 4y - 5 =0	Solve the system of equations: x + 5y + 2z = 0 2x + 8y + 3z = 1 -x - y + 2z = 0	How many ways can the Caltech Ultimate frisbee team choose a starting lineup of 7 people from a group of 10?	Evaluate: 396 times 404	The Mathketeers hike 3 miles north of Eigen lake, then 8 miles east, then 7 miles south, then 10 miles west in time for dinner. How far, in miles, are they from Eigen Lake?	A string long enough to fit exactly around a square with diagonal $6\sqrt{2}$ also fits exactly around a circle. What is the radius of the circle?	How many vertical asymptotes does $f(x) = \frac{4}{x^2 + 1}$ have? Read as: How many vertical asymptotes does f of x equals 4 divided by the quantity x squared plus 1 have?	College Knowledge Bowl Questions #2
4/27	:	(0,1) and (0, -5)	х = 3, У = -1,	120	159984	2√5 [mi]	12/π	0 or none	

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Solve for x: Figure not drawn to scale. x
What is the area of the triangle with vertices at (4, 1), (-1, 7), and (-3, -2)?
Evaluate: 2003³ - 2002³.
If each side of a certain equilateral triangle decreases by 2 inches, the area decreases by $5\sqrt{3}$ /2 square inches. What was the original area, in square inches, of the triangle?
Using the equation for a plane passing through the points (3,0,0) (0,-4,0) and (0,0,5) in the form $Ax + By + Cz = D$, where the greatest common divisor of A , B , C , and D is 1 and D is pasitive, find $A + B + C + D$.

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Express all answers in terms of radicals and π_{r} where applicable, unless otherwise instructed.

Pers	Person #1	
-	How many prime numbers less than 30 are divisible by 3?	-1
73	Evaluate: $\sqrt{8^2+15^2}$ Read as: Evaluate the square root of the quantity eight squared plus fifteen squared	17
ω	What is the geometric mean of 12 and 1082	36
4	Solve for x: 2" = 1024 Read as: solve for x: two to the power x equals 1024.	[×=]10
Pers	Person #2	
-	What is the measure, in degrees, of one interior angle of a regular pentagon?	108[°]
2	What is the sum of the reciprocals of the first three primes?	31/30
ω	What is the surface area of a sphere with radius 💤	п
4	Solve for $x: 2x^2 - 3x + 1 = 0$ Read as: Solve for $x:$ two times x squared minus 3 times x plus 1 equals zero.	x=1 or x=1/2 Both answers needed
Pers	Person #3	
	What is the slope of a line with x-intercept (12, 0) and y-intercept (0, 8)?	-2/3
2	What is the greatest common factor of 196 and 280?	28
ću	What is the maximum passible volume of a rectangular prism with a surface area of 24 square centimeters?	8 [cm²]
4-	If the sum of three consecutive integers is 1560, what is the largest number?	521
Pers	Person #4	
1	How many diagonals can be drawn in a regular octagon?	20
2	If $a+b=90$, and a and b are both primes, what is the largest possible value of a?	83
ω	Write as a repeating decimal: 6/11	.545454 or
4	A cylinder filled with maple syrup has a radius of 2 and a height of 27. If it is emptied into 3 congruent spheres, and each are completely filled, what is the radii of the spheres?	ω

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	College Knowledge Bowl Questions #3	
	What is the least common multiple of 48, 36, and 45?	720
2	What is the sum of the first 12 odd numbers?	144
ω	Express 172 in base 2.	10101100
4	Simplify: $i^{19} + i^{82} + i^7 + i^{29}$	-1-/
ΟI	At which points do $y = x^2$ and $y = 3x - 2$ intersect?	(1,1) and (2,4)
6	What is the area of a regular hexagon with side length 2?	6√3
7	For what value of c does $2x^2 + 8x + c = 0$ have exactly one real solution?	c=8
	Number $oldsymbol{arrho}$ is an extra question. Only use it if needed.	
00	How many multiples of 13 are between 3000 and 4000?	77

MIGHT IS COOL MIGSTERS -- COUS

School Name____ Proctor Name___ 9th and 10th Grade - May 10

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Individual Contest - Score Sheet	Name:
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"Math is Cool" Masters -- 2003 9th and 10th Grade - May 10, 2003

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										-1, 0 or 2
										-1, 0 or 2

4. (2a-3b-c)(2a+3b+c) 8. 28

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y = -2/3x + 48:5 or 8/5

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Math is Cool" Masters -- 2003 9th and 10th Grade - May 10, 2003

Team Contest-Score Sheet

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Pressure Round - Score Sheet

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[x =] 5	57/2 or 28.5 or 28 ½	12,030,019	$\frac{49\sqrt{3}}{16}$ [square inches]	77	Answer
		:			